

PHYS 110

TECHNICAL PHYSICS

STUDENT WORKBOOK

(3rd Edition revised Dec 2020)

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USN – retired



Page Heading	Page #
About this notebook	
Scientific Notation	1
Positive Exponents	2
“zero” power	3
Self-check	4
Additional exercises	5
Converting numbers	6
Self check	7
Operations in Scientific Notation	8
Division	9
Addition/Subtraction	10
Squaring numbers	11
Square roots	12
Metric System	13
Commonly used metric prefixes	14
Self check	15
Self check	16
Converting metric prefixes	17
Example 2	18
Example 3	19
Self check	20
Physics terms	21
Mass	22
Self check	23
Conversions	24
Applying method of multiplying fractions	25
Step 7: restate with remaining terms	26
Algebraic equations: Cross-multiplying	27
Self check	28
Field shorthand method (Navy Egg)	29
Example 4	30
Example 4 (continued)	31
Self check	32
Historical Figures	32a
Historical Figures (cont)	32b

Historical Figures (cont)	32c
Historical Figures - self -check	32d
The Scientific Method	32e
The Scientific Method (cont)	32f
Scientific Method Flow Chart	32g
Key Points - Scientific Method	32h
Structure of atom	33
Example 2 – Helium atom	34
Volume	35
Mass Density Calculations	36
Example 2: Predicting the mass	37
Step 4: cross-multiply	38
Self check	39
Vectors	40
Example 1: Two bungee cords	41
Example 3: Two bungee cords	42
Basic Right-Angle Trigonometry	43
“Theta”	44
Sine	45
Example 1	46
Example 2	47
Example 3	48
Solution for “H”	49
Practical principles	50
Example	51
Using the ____ of tangent	52
(Omitted)	(53)
Adding Vectors	54
V_2 , 6.3 Newtons, 63°	55
Example 2:	56

Example 3	57
Forces in Equilibrium	58
Force Table Lab and the Scientific Method	59
7. Construct model	60
Vectors Overview (cont.)	61
Motion	62
4. Acceleration	63
Acceleration (continued)	64
Example 1: Beach Bucket	65
Critical Factors in Acceleration Calculations	66
Basic Formulas Used in Acceleration Problems	67
Basic Formula:	68
Basic Formula:	69
Refined List of Variants of Basic Formulas	70
Working through acceleration formulas	71
Example 2	72
Example 3	73
Example 4	74
Part 3	75
Acceleration: Ball go up, ball come down	76
Example 1:	77
Example 2	78
Study/Practice Sheet 1	79
VI. MASS DENSITY (D_m)	80
Study/Practice sheet 3	81
Projectile Motion	82
Projectile Motion Elevation: 0°	83
Projectile Motion Worksheet	84
Projectile Motion Lab Worksheet	85
Trebuchet Worksheet	86

Work, Energy and Power	87
The role of trigonometry in evaluating “work”	88
Power	89
Energy	90
Simple Machines (Overview)	91
Simple Machines	92
Class ____ Lever	93
The Inclined Plane	94
The Screw	95
The Pulley	96
The Pulley (cont.)	97
The Wedge	98
Sound	100
Sound (cont.) Example 1	101
Sound (cont.) the role of the medium	102
The Doppler Effect	103
Doppler Effect – Passive Sonar	104
Doppler Effect - Light	105
Wiley Coyote	106
Relativity	107
Michelson – Morley	108
Einstein - Lorentz Transformations	109
Understanding “Gamma”	109a
Gamma chart for relativistic velocities	109b
Gamma chart for relativistic velocities (pt2)	109c
Einstein (cont.)	110
Einstein – “Lorentz Factors”	111
Example 1	112
Relativity and the muon	113
The Twins Paradox	113a

Extreme Time Travel	113b
Practical Problems with Relativistic Velocityex1	113c
Practical Problems with Relativistic Velocity ex2	113d
The New Physics	113e
Relativity, Light and Gravity	114
Solar Eclipse	115
The Relationship of Mass and Energy	116

ABOUT THIS WORKBOOK

This book is based on the formatted notebook model used by United States Navy class “A” technical schools. This format is a well proven and time-tested method of instruction; no fluff, no filler, and yet comprehensive and thorough.

For example, this method allows a Navy student to complete a *fully transferrable undergraduate level three-credit course in Oceanography in two weeks!*

Key points in this format:

1. It minimizes the potential for ambiguity and enables the student to more effectively identify key points in a given lecture
2. It enables the student to more effectively “compare notes” with classmates
3. Both student and instructor are literally “on the same page.”
4. Student **ownership** of specific course information is clearly delineated
5. It **WORKS!**

Topic/Lab 1: SCIENTIFIC NOTATION

Scientific Notation: Provides a means of managing and calculating _____ and _____ numbers.

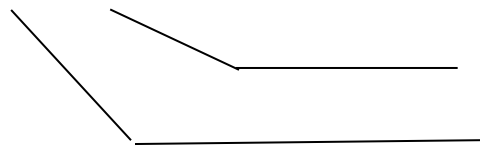
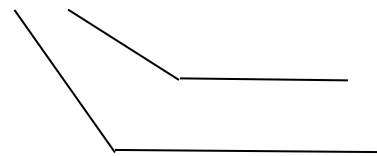
Based on an understanding of _____ and the _____

Algebra:

Scientific Notation:

$$3 \times 2 \text{ _____}$$

$$3 \times 10^2 \text{ _____}$$



The same rules pertaining to _____ , _____ and _____ in Scientific Notation also apply in algebra.

Coefficient:

Base:

Exponent:



**Oog, the
Cave Man**

Positive Exponents

Let's start with the easy stuff - multiplication:



Why physics teachers should not be given playground duty

Negative Exponents

Bottom line:

A negative exponent means you're dealing with a _____ or a _____

“Zero” power: (x^0)

Any non-zero number to the “zero power” equals _____

Rationale:

First power: (x^1)

Any number to the 1st power equals _____

Standard Notation:

Lab exercises:

$3.8^0 =$	
$3.8 \times 10^0 =$	
$3.8^1 =$	
$3.8 \times 10^1 =$	
$5^3 =$ (standard notation)	
$672 \times 10^3 =$ (standard notation)	
$6^{-2} =$ (include both possible answers)	
In the expression " 3.12×10^4 " the "3.12" is called the _____	
$9.36^{-1} =$	
$x^5 \times x^7 =$	
$y^6 \div y^4 =$	
$53^0 =$	
$87^1 =$	
$2.38 \times 10^0 =$	
Definition of an exponent:	
In the expression " 8.75×10^7 " the "10" is called the _____	
A negative exponent indicates you're dealing with a _____ or a _____	
$5^{15} \times 5^{-17} =$ (include all possible answers)	

L R

Converting numbers in standard notation to scientific notation

If the decimal point moves to the _____, the exponent goes _____

If the decimal point moves to the _____, the exponent goes _____

Converting numbers in Scientific Notation to Standard Notation

If the exponent moves _____, the decimal point moves _____

If the exponent moves _____, the decimal point moves _____

“Cheater Rule” for Standard Notation:

Any number in standard notation can be expressed as _____ times _____

General Rule for correct scientific notation:

“Only one _____ in the _____ to the _____ of the decimal”

Very Important Exception:

It is often more convenient to ignore this rule during _____

(In other words, don't get hung up on this and create more problems than necessary)

<p>Example 1: Convert 873.463 into correct scientific notation</p>	<p>Example 2: Convert 0.00785 into correct scientific notation</p>	<p>Example3: Convert 56.98×10^5 into correct scientific notation</p>
---	---	---

Convert to correct scientific notation:

186,000	0.0045
5280	34.78×10^3
783.487×10^{-8}	2.85
0.000859×10^{-9}	0.0835×10^6
0.0000386×10^{12}	73.96
1/4	.937

Convert to standard notation:

1.63×10^3	3.637×10^{-1}
2.94×10^{-6}	36.345×10^2

Operations in Scientific Notation

Multiplication Critical Rules:

Multiply _____

Retain _____

Add _____

NOTE:

Adding a negative number is the same as _____ a _____ _____

Example 1:

$$(4.75 \times 10^3) \times (2.43 \times 10^7)$$

Example 2:

$$(3.72 \times 10^7) \times 1.67 \times 10^{-2}$$

Division Critical Rules:

Divide _____

Retain _____

Subtract _____

NOTE:

Subtracting a negative number is the same as _____ a _____ _____

Example 1:

$$(9.35 \times 10^8) \div (3.54 \times 10^4)$$

Example 2:

$$(8.62 \times 10^6) \div (3.97 \times 10^{-3})$$

Addition/Subtraction Critical Rules:

Exponents _____

Add/Subtract _____

Retain _____

Retain _____

Example 1:

$$(6.72 \times 10^3) + (2.97 \times 10^3)$$

Example 2 :

$$(9.56 \times 10^5) - (8.47 \times 10^4)$$

Squaring and Cubing numbers in Scientific Notation - Critical Rules

Square / Cube _____

Retain _____

Multiply _____ by _____ or _____

RECALL:

Multiplying unlike signs results in a _____

Multiplying like signs results in a _____

Example 1: $(2.56 \times 10^3)^2$	Example 2: $(2.56 \times 10^3)^3$
Example 3: $(3.12 \times 10^{-6})^2$	Example 4: $(3.12 \times 10^{-6})^3$

Square Roots/Cube Roots in Scientific Notation - Critical Rules

Exponent must be divisible by _____ or _____

Square/Cube root _____

Retain _____

Divide _____ by _____ or _____

RECALL:

Dividing unlike signs results in a _____

Dividing like signs results in a _____

<p>Example 1:</p> $\sqrt{9.46 \times 10^6}$	<p>Example 2:</p> $\sqrt[3]{9.46 \times 10^6}$
<p>Example 3:</p> $\sqrt{8.1 \times 10^5}$	<p>Example 4:</p> $\sqrt[3]{8.1 \times 10^5}$

$(3.93 \times 10^7) \times (5.37 \times 10^6)$	Answer:
$(3.92 \times 10^3) \times (3.48 \times 10^{-5})$	Answer:
$(8.14 \times 10^7) \div (4.05 \times 10^9)$	Answer:
$(8.16 \times 10^{-5}) \div (4.89 \times 10^6)$	Answer:

$(3.93 \times 10^7) \times (5.37 \times 10^6)$ $\begin{array}{r} 3.93 \times 10^7 \\ 5.37 \times 10^6 \\ \hline 21.104 \times 10^{13} \\ = 2.1104 \times 10^{14} \end{array}$	2.1104×10^{14}
$(3.92 \times 10^3) \times (3.48 \times 10^{-5})$ $\begin{array}{r} 3.92 \times 10^3 \\ 3.48 \times 10^{-5} \\ \hline 13.642 \times 10^{-2} \\ = 1.364 \times 10^{-1} \end{array}$	1.364×10^{-1}
$(8.14 \times 10^7) \div (4.05 \times 10^9)$ $\begin{array}{r} 8.14 \times 10^7 \\ 4.05 \times 10^9 \\ \hline \\ = 2.0098 \times 10^{-2} \end{array}$	2.0098×10^{-2}
$(8.16 \times 10^{-5}) \div (4.89 \times 10^6)$ $\begin{array}{r} 8.16 \times 10^{-5} \\ 4.89 \times 10^6 \\ \hline \\ = 1.669 \times 10^{-11} \end{array}$	1.669×10^{-11}

$\sqrt{2.36 \times 10^7}$	
$(2.64 \times 10^7) (1.37 \times 10^7)$	
$(3.93 \times 10^7)^2$	
$(5.37 \times 10^6)^3$	
$\sqrt{8.26 \times 10^8}$	
$\sqrt[3]{5.06 \times 10^{16}}$	

$\sqrt{2.36 \times 10^7}$ <p>Change to : $\sqrt{23.6 \times 10^6}$ (exponent divisible by 2)</p> $= 4.858 \times 10^3$	4.858×10^3
$(2.64 \times 10^7) - (1.37 \times 10^7)$ $\begin{array}{r} 2.64 \times 10^7 \\ -1.37 \times 10^7 \\ \hline 1.27 \times 10^7 \end{array}$	1.27×10^7
$(3.93 \times 10^7)^2$ $= 15.445 \times 10^{14}$ $= 1.5445 \times 10^{15}$	1.5445×10^{15}
$(5.37 \times 10^6)^3$ $= 154.854 \times 10^{18}$ $= 1.54854 \times 10^{20}$	1.5485×10^{20}
$\sqrt{8.26 \times 10^8}$ 2.874×10^4	2.874×10^4
$\sqrt[3]{5.06 \times 10^{16}}$ <p>change to: $\sqrt[3]{50.6 \times 10^{15}}$ (exponent divisible by 3)</p> $= 3.699 \times 10^5$	3.699×10^5

Metric System

Major advantage of the metric system:

It can be applied directly to _____

Uses a system of _____ and _____

Units relate to specific _____ (“whatcha got”)

Prefixes are specific _____ (“how many you got”)

Prefixes are mathematically _____ with _____ of _____

Examples of units:

Examples of prefixes:

UNIT:	MEASUREMENT OF:	PREFIX:	EQUIVALENT:
Meter	_____	Centi	_____ or _____
Liter	_____	Milli	_____ or _____
Gram	_____	Kilo	_____ or _____

Hence:

8.5 centimeters = 8.5 x _____ meters

500 milliliters = 500 x _____ liters

6.75 kilograms = 6.75 x _____ grams

BOTTOM LINE:

Any prefix can be replaced or substituted with a _____ of _____

self check:

centi = (standard notation)	
kilo = (power of ten)	
10^9 = (prefix)	
10^{-3} = (standard notation)	
0.01 = (prefix)	
giga = (power of ten)	
1000 = (power of ten)	
10^6 = standard notation)	
milli = (power of ten)	
micro = (standard notation)	
10^{-2} = (prefix)	
0.001 = (power of ten)	
10^3 = (prefix)	
mega = (standard notation)	
milli = (standard notation)	
1,000,000 = (power of ten)	
0.000001 = (power of ten)	
kilo = standard notation	
10^6 = (prefix)	
1,000,000,000 = (power of ten)	

Informal Lab Exercise:

	Scientific Notation	Standard Notation
8.97 kilograms = ? grams		
6.5 centimeters = ? meters		
7.5 gigavolts = ? volts		
4.7 microFarads = ? Farads		
6.4 megawatts = ? watts		
9.87 milliliters = ? liters		

Quantity:**Equivalent quantity with prefix**

5483 grams	
0.0268 meters	
9,700,000,000 volts	
0.0000056 Farads	
0.0045 liters	
4,300,000 watts	

Conversion hack:

Convert 3.567×10^5 gigavolts to millivolts

Self - check

(Answer in correct scientific notation)

5.98×10^4 kilograms = _?_ grams	
8.34×10^{-1} meters = _?_ centimeters	
5.92×10^{-4} megawatts = _?_ watts	

(Answer in standard notation:)

500 millivolts = _?_ volts	
345 grams = _?_ kilograms	
6.73×10^5 centimeters = _?_ meters	
3.81×10^{-4} volts = _?_ microvolts	

(Answer in correct scientific notation:)

3.45×10^5 microvolts = _?_ kilovolts	
7.93×10^{-5} kilograms = _?_ milligrams	
5.78×10^3 millimeters = _?_ centimeters	
4.32×10^3 gigahertz = _?_ megahertz	

Physics terms

Displacement:

Definition(s):

1. _____ and _____

2. _____ and _____

Symbol: _____

Standard units:

1. British ("U.S Standard"): _____

2. Metric: _____

NOTE: In this context "displacement" does NOT refer to _____

Force:

Definition(s):

1. _____ or a _____

2. That which may _____

Symbol: _____ (Weight is a measure of _____)

Standard units:

1. British ("English"): _____

2. Metric: _____

NOTE:

Since a _____ is a unit of force, then it is NOT a measure of _____ .

Mass:

Definition(s):

1. _____
2. _____ *
3. _____

* “ _____ ” : resistance to a _____ in _____

Standard units:

1. British: _____ (not _____)
2. Metric: _____ / _____ (not _____)

Volume:

Definition:

1. _____

Standard units:

1. British: _____ (_____)
2. Metric: _____ (_____)*

* NOTE: “ _____ ” are also frequently used to measure volume in metric terms, but are no longer considered as “standard units.”

Time:

Definition:

1. “That which we _____ ”
- _____

Standard unit: (both British and metric)

1. _____ (NOT _____ or _____)

self check:

Answers:

a measure of inertia	
that which we measure with a clock	
distance and direction	
standard metric unit of force	
standard British unit of displacement	
a quantity of space	
standard metric unit of mass	
a push or a pull	
length and direction	
standard British unit of force	
standard metric unit of volume	
that which may affect motion	
weight is a measure of _?_	
resistance to a change in motion	
standard British unit of volume	
standard British unit of mass	
standard unit of time	
standard metric unit of displacement	
a quantity of material	
stuff	

CONVERSIONS

Based on the principles used in _____ , and

exploit the rules used in “ _____ - _____ ”

Example 1:

$$\frac{3}{4} \times \frac{1}{3} =$$

Example 2:

$$\frac{a}{c} \times \frac{b}{a} =$$

Example 3:

$$\frac{\bigcirc}{\square} \times \frac{\triangle}{\bigcirc} =$$

Rationale:

Applying method of multiplying fractions as a means of converting units
(The “factor-labeling” method)

Example 1:

To convert 35 miles per hour to “x” feet per second :

Step 1: Restate 35 MPH in fraction form:

$$\frac{35 \text{ miles}}{1 \text{ hour}}$$

Step 2: Set up multiplication problem in fraction form so that the terms you wish to change will be _____ - _____ :

$$\frac{35 \text{ mi}}{1 \text{ hour}} \times \frac{\quad}{\text{mi}} \times \frac{\text{hour}}{\quad}$$

Step 3: Replace terms with those you want:

$$\frac{35 \text{ mi}}{1 \text{ hour}} \times \frac{\text{feet}}{\text{mi}} \times \frac{\text{hour}}{\text{seconds}}$$

Step 4: Inert correct mathematical equivalences:

$$\frac{35 \text{ mi}}{1 \text{ hour}} \times \frac{5.28 \times 10^3 \text{ feet}}{1 \text{ mi}} \times \frac{1 \text{ hour}}{3.6 \times 10^3 \text{ sec}}$$

Step 5: Cross-cancel terms:

$$\frac{35 \text{ miles}}{1 \text{ hour}} \times \frac{5.28 \times 10^3 \text{ feet}}{1 \text{ mile}} \times \frac{1 \text{ hour}}{3.6 \times 10^3 \text{ sec}}$$

Step 6: Restate with remaining terms:

$$\frac{35 \times 5.28 \text{ feet}}{3.6 \text{ sec}}$$

Step 7: Perform normal calculations *one operation at a time* until you reach an answer in the desired terms*

$$\frac{35 \times 5.28 \text{ feet}}{3.6 \text{ sec}} = \frac{184.8 \text{ feet}}{3.6 \text{ secs}} =$$

_____ * **ft/sec** (final answer)

Conversion factors you should know:

1 mile = 5.28×10^3 ft

1 mile = 1.61×10^3 meters

1 kilometer = 10^3 meters

1 hour = 3.6×10^3 seconds

Self-check: conversions

Answers:

Convert 400 MPH to ft/sec

Convert 80 meters/sec to miles/hour

Convert 220 ft/sec to MPH

Convert 88 kilometers/hr to meters/sec

Field - shorthand method for algebraic equations (Navy "egg")

Example 1

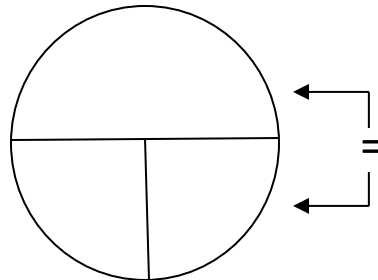
Given: "12", "3", and "4"
then:

$$\frac{12}{3} = 4$$

$$\frac{12}{4} = 3$$

and $3 \times 4 = 12$

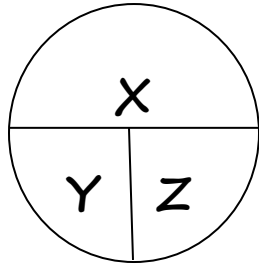
Or:



X

Example 2

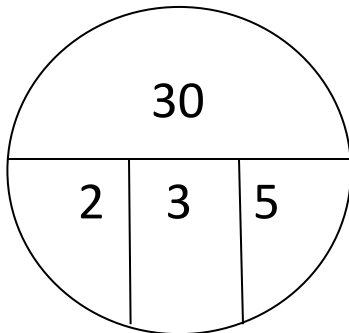
Given:



Then:

Example 3

Given:



Then: 30 = _____

2 = _____

3 = _____

5 = _____

"People, listen up!
There is the Right Way,
there is the Wrong Way,
and then there is the Navy Way,
and you better start learning the Navy Way!"

-Boatswain's Mate Second Class Donald Barger, USN,
Navy Boot Camp Company Commander



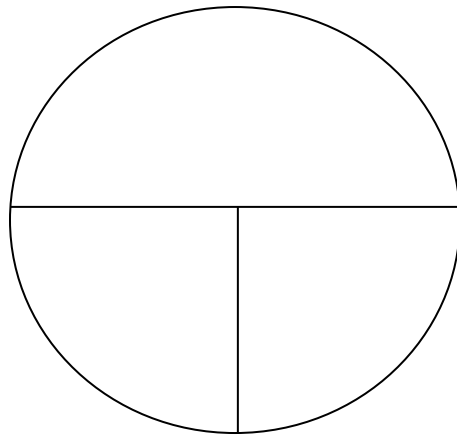
Example 4:

Given: $\frac{ab}{cde} = fg$ Solve for "d"

Traditional solution:

Using the "egg"

$\frac{ab}{cde} = fg$, Solve for "d"



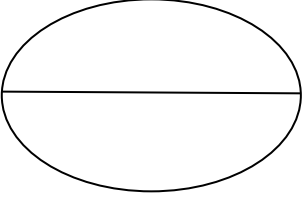
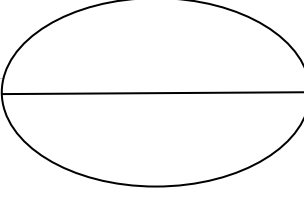
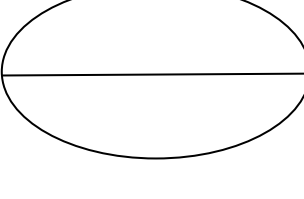
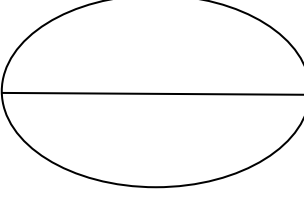
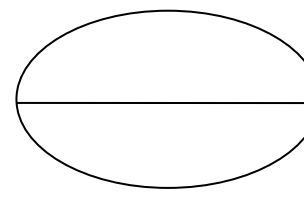
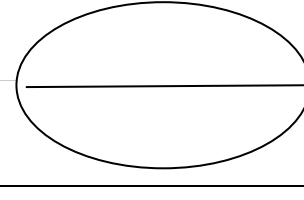
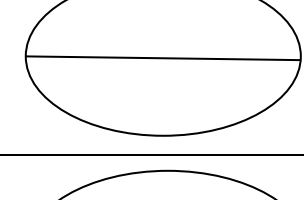
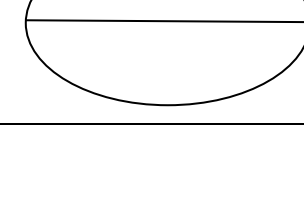
$d = \underline{\hspace{2cm}}$

Self check:

Equation:

"Egg"

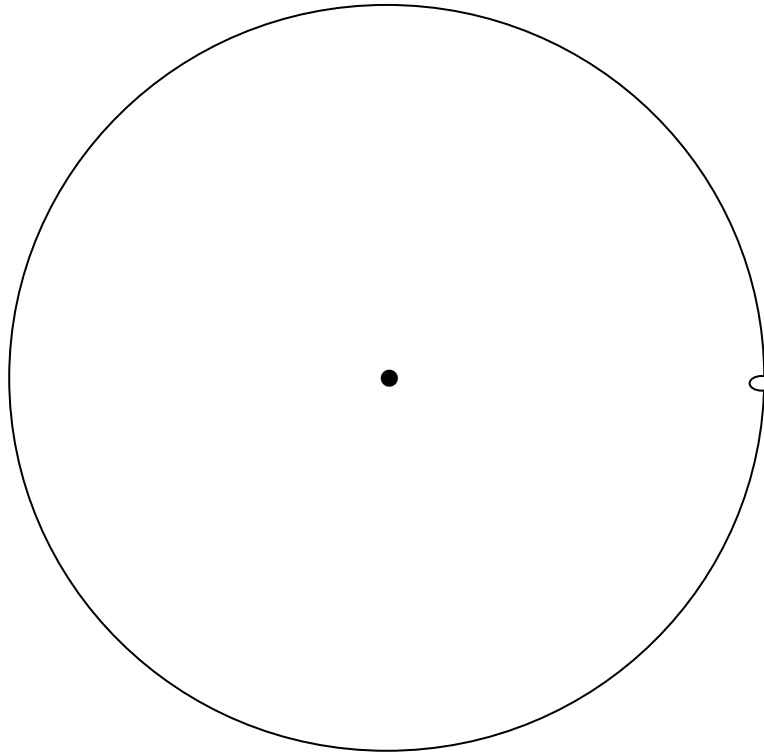
Solution ("n" = ?)

$F = ma$		$m =$
$P = \frac{W}{T}$		$T =$
$2as = (V_f^2 - V_i^2)$		$a =$
$KE = \frac{1}{2}mv^2$ (Hint: $\frac{1}{2} = .5$)		$m =$
$D = R \times T$		$T =$
$PE = mgh$		$h =$
$A = (\cos \theta)(H)$		$H =$
$a = \frac{V_f - V_i}{t}$		$t =$

Structure of atom - a key to understanding "mass"

Example 1:

Hydrogen:



Proton:

1. _____ charge
2. Has approximately _____ times the mass of electron

Electron:

1. _____ charge

Hydrogen:

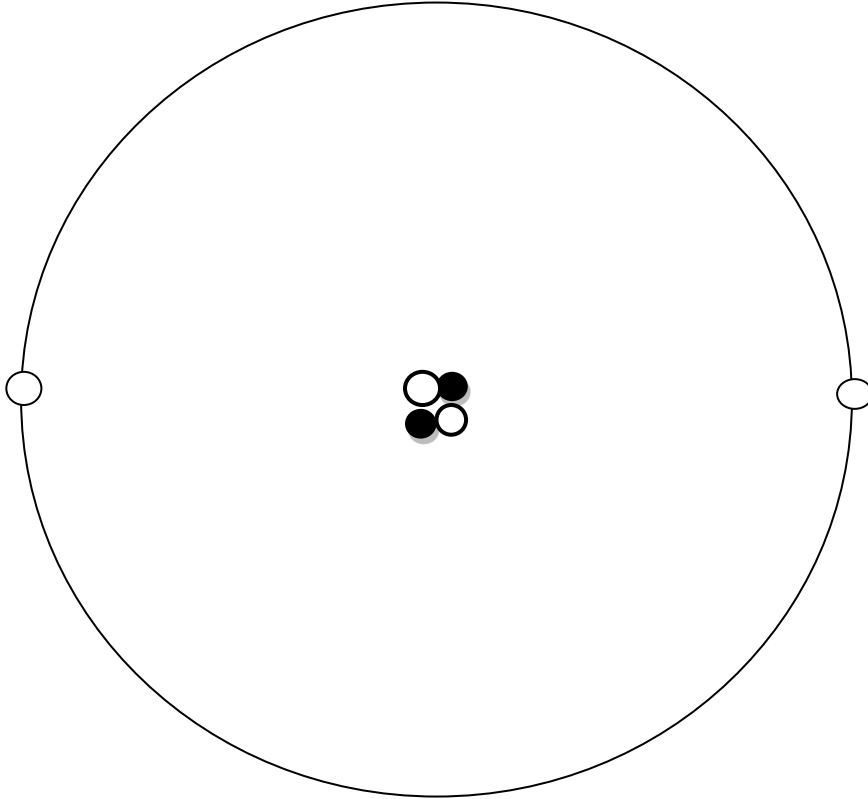
1. _____ of all atoms
2. _____ element in the universe

"There is more stupidity than hydrogen in the universe, and it has a longer shelf life."

- Frank Zappa



Example 2 - Helium atom

*(NOT to scale!)*

Nucleus:

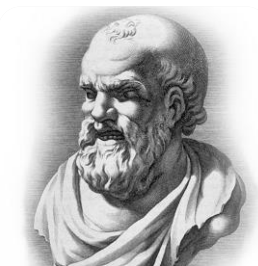
1. Contains _____ and _____
2. Accounts for _____ of atom's mass

Neutron:

1. Slightly more _____ than a proton, hence it also has
approximately _____ times the mass of electron
2. _____ charge

By volume, an atom is over _____ percent _____

Atom Model History

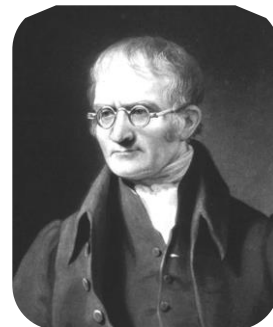


Democritus - Fifth century B.C.

1. All matter is composed of _____
2. "Atom" : Greek for " _____ "

John Dalton - 1803

1. Atom is a _____
(AKA the " _____ model")
2. Each element was composed of _____
3. Different elements composed of _____
4. Compounds are composed of atoms in _____
5. Chemical reactions are _____ of _____ ,
And mass is therefore _____ .

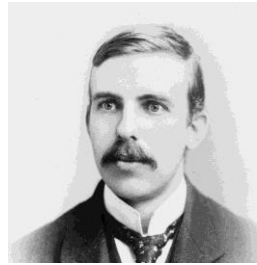


Joseph John Thompson - 1897

1. "Plum _____ " _____ :
a. A sphere of diffuse _____ electricity with
negative _____ imbedded throughout
2. Discovered _____ , and was awarded _____ in 1906



The "Solar System" Model



Ernest Rutherford - 1911

- 1. Discovered that the atom is mostly _____ with a dense _____ charged _____ surrounded by negative _____

Neils Bohr - 1913



- 1. Electrons travel in _____
- 2. Only _____ allowed
- 3. Modern _____ of the _____

"Everything we call real is made of things that cannot be regarded as real."
~Niels Bohr

Electron Cloud Model - 1920's

- 1. **Erwin Schrodinger¹** and **Werner Heisenberg²**

Developed _____ functions to determine regions or clouds in which _____ are most likely to be found

- 2. Heisenberg: Developed the _____ Principle : Impossible to predict _____ of single electron

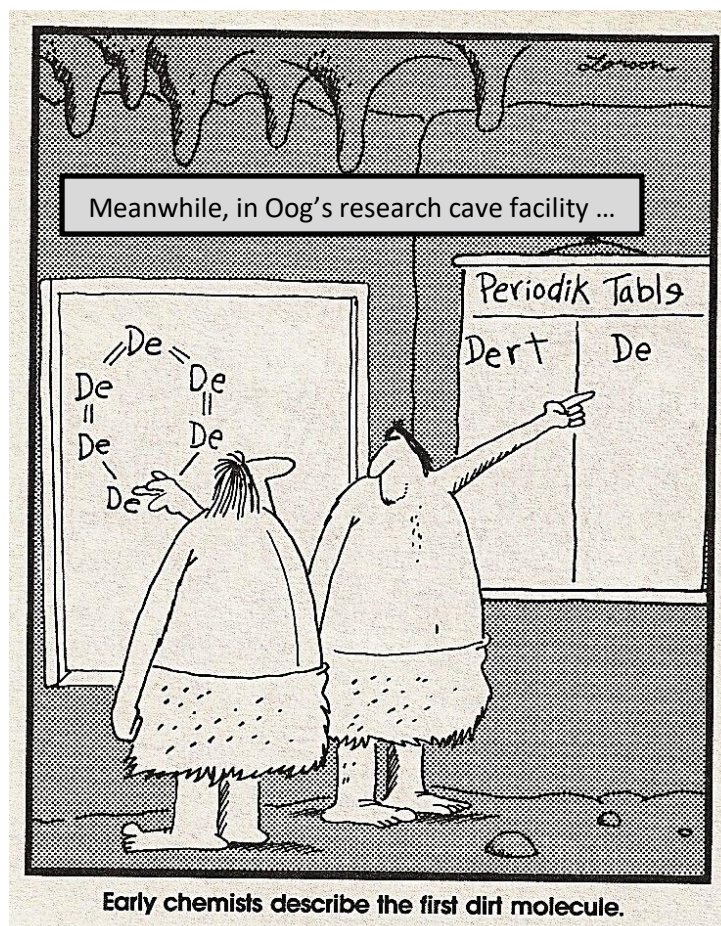


James Chadwick - 1932

- 1. British experimental physicist credited with discovering the _____

Particles and average radii:

Particle	Approx. Radius
	10^{-9} meters
	10^{-10} meters
	10^{-15} - 10^{-14} meters
	10^{-15} meters
	10^{-18} meters



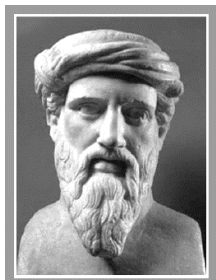
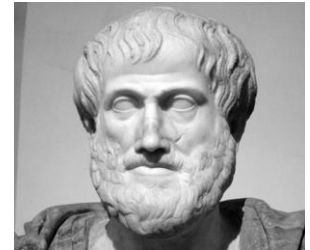
More History: How We Got Here

The 3-legged stool of understanding is held up by history, languages, and mathematics. Equipped with these three you can learn anything you want to learn. But if you lack any one of them you are just another ignorant peasant with dung on your boots.

- Robert A. Heinlein, author, engineer, U.S. Naval Academy graduate, curmudgeon.

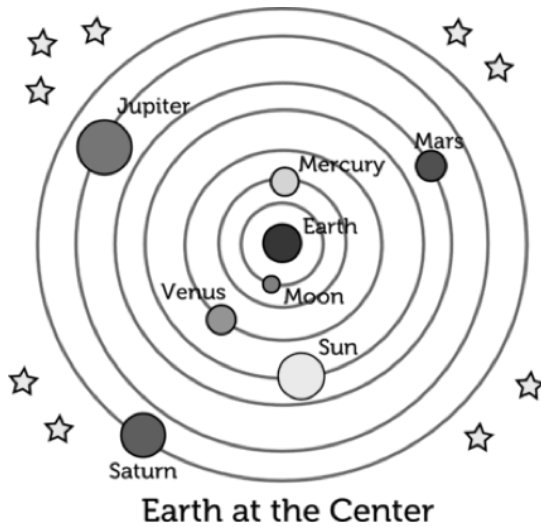
Aristotle

1. _____
2. _____
3. _____
4. _____

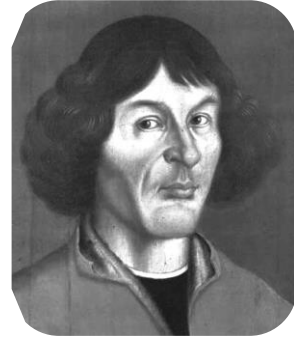


Pythagoras

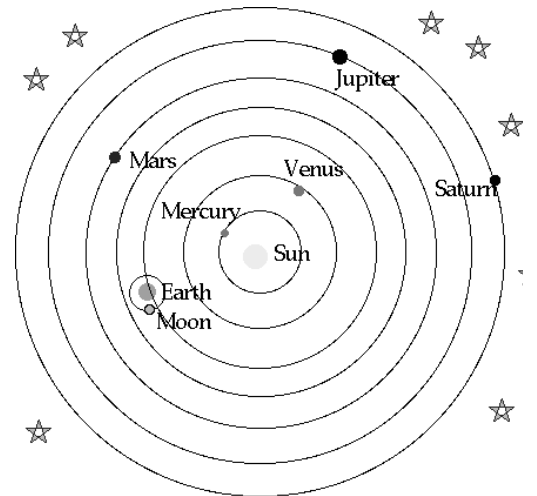
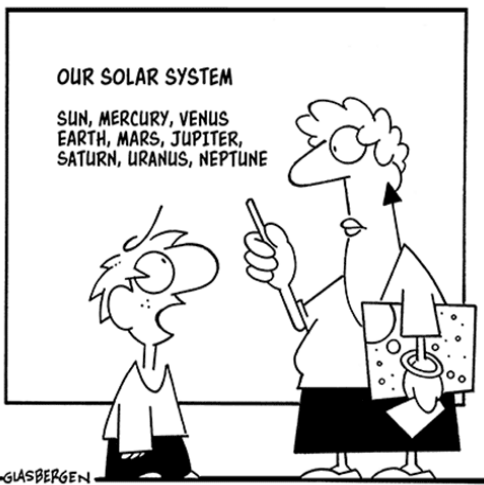
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-
-



Copernicus



1. _____
2. _____
3. _____
4. _____



“Until I see evidence to the contrary, I will continue to believe that **I** am the center of the universe.”

Galileo

1. First to use the _____

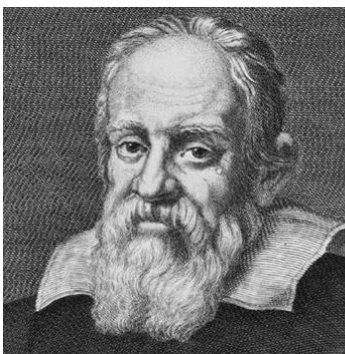
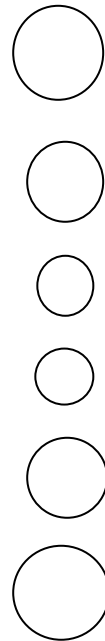
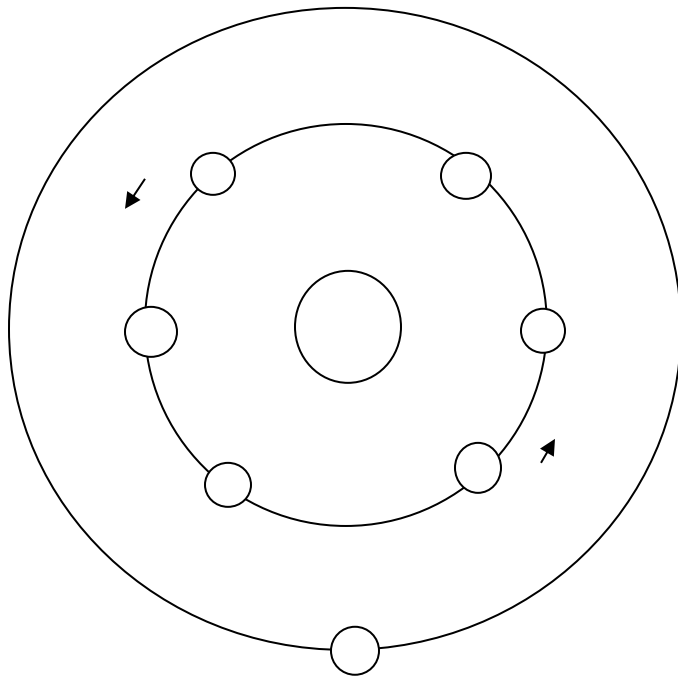
2. Discovered the _____ of _____

3. Discovered the _____ of _____

4. Discovered _____

4. Prime author of the _____

5. Was tried for _____



GALILEO DESCRIBES HIS DISCOVERIES TO THE CHURCH

Sir Isaac Newton:

1. Wrote _____

2. Discovered _____

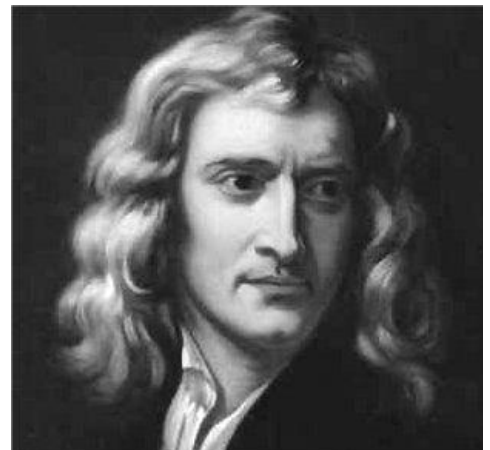
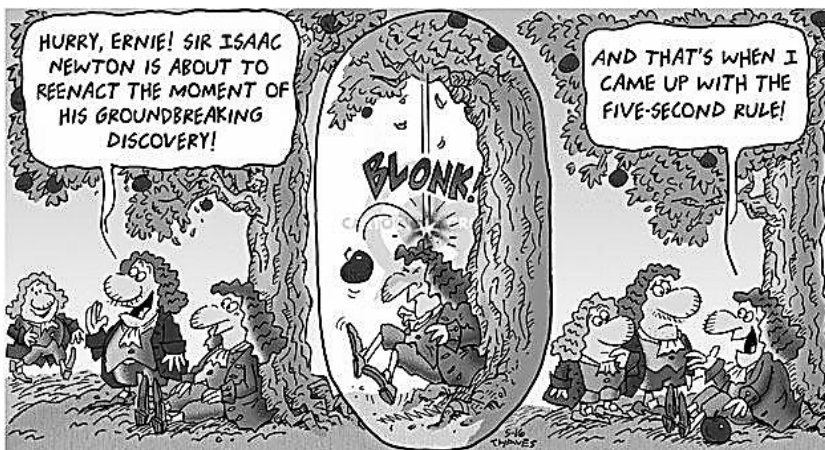
3. Established the link _____

4. Sought to _____

5. Emphasized A _____ , _____ results@

6. Invented _____

7. Derived planetary motions _____



The Scientific Method

“Physicists are conservative revolutionaries. They do not give up tried and tested principles until experimental evidence - or an appeal to logical and conceptual simplicity - forces them into a new and sometimes revolutionary viewpoint. Such conservatism is at the core of the critical structure of inquiry. Pseudoscientists lack that commitment to existing principles, preferring instead to introduce all sorts of ideas from the outside.”

- Dr. Heinz R. Pagels, “The Cosmic Code”

If it walks like duck, swims like duck, quacks like duck . . . it’s probably not an elephant.”

- Chief Petty Officer Ralph Caraway, Master Instructor, USN-retired, explaining the overarching theory of acoustic intelligence analysis.

You can observe a lot just by watching.”

-Yogi Berra, American philosopher

The Scientific Method is a remarkably adaptable tool that allows us “mere mortals” to pursue the most profound truths. Its strength lies in both its beautifully articulated process and its flexibility.

We keep the Scientific Method around because it works, and most importantly, it has **never failed**. Not even once. Its self-correcting nature prohibits failure.

Now that’s a pretty bold if not outrageous statement, so let’s bring the topic into sharper focus by stipulating a distinction between the “Scientific Method” and “Science” itself:

While the Scientific Method does not fail, Science often does. It happens all the time, and is a normal, entirely expected part of the business. The Scientific Method gives us the means to (1) recognize and deal with these failures and (2) establish the credibility of successes through a rigorous, clearly defined vetting process.

In short, the Scientific Method is how we police the business of Science.

Though frequently viewed as an esoteric, intellectual protocol, it also has very practical, down-to-earth applications. One beautiful example of this (I believe) is the grand experiment of American Democracy. People a lot smarter and more credentialed than me have long argued that it’s no coincidence that the architects of the American government were also products of the Galilean/Newtonian revolution of scientific rationale (think Thomas Jefferson and Benjamin Franklin, both well-established scientists, inventors, and philosophers in their own right). Look closely, and you will see a remarkable similarity between the Scientific Method and our constitutional system of informed candid debate, peer review, accountability and a formal regimen of “checks and balances.”

Both protocols are ultimately beholden to unvarnished reality, and survive the most rigorous challenges to their very existence because they are specifically engineered as fluid, adaptive processes of deliberative, critical analysis and self-correction.

“Galileo was one of the first people to practice what we recognize today as the scientific process (or “method”): the dynamic interplay between experience (in the form of experiments and observations)

and thought (in the form of creatively constructed theories and hypotheses). This notion that scientists

learn not from authority or from inherited beliefs but rather from experience and rational thought is what makes Galileo’s work, and science itself, so powerful and enduring.

“Galileo’s methods have been crucial to science ever since. They included:

- *Experiments*, designed to test specific hypotheses
- *Idealizations* of real-world conditions, to eliminate (at least in ones’s mind) any side effects that might obscure the main effects
- *Limiting the scope of inquiry* by considering only one question at a time. For example, Galileo separated horizontal from vertical motion, studying only one of them at a time.
- *Quantitative methods*. Galileo went to great lengths to measure the motion of bodies. He understood that a theory capable of making quantitative predictions was more powerful than one that could make only descriptive predictions, because quantitative predictions were more specific and could be experimentally tested in greater detail

“**Observation** refers to the data gathering process. A **measurement** is a quantitative observation, and an **experiment** is an observation that is designed and controlled by humans, perhaps in a laboratory.

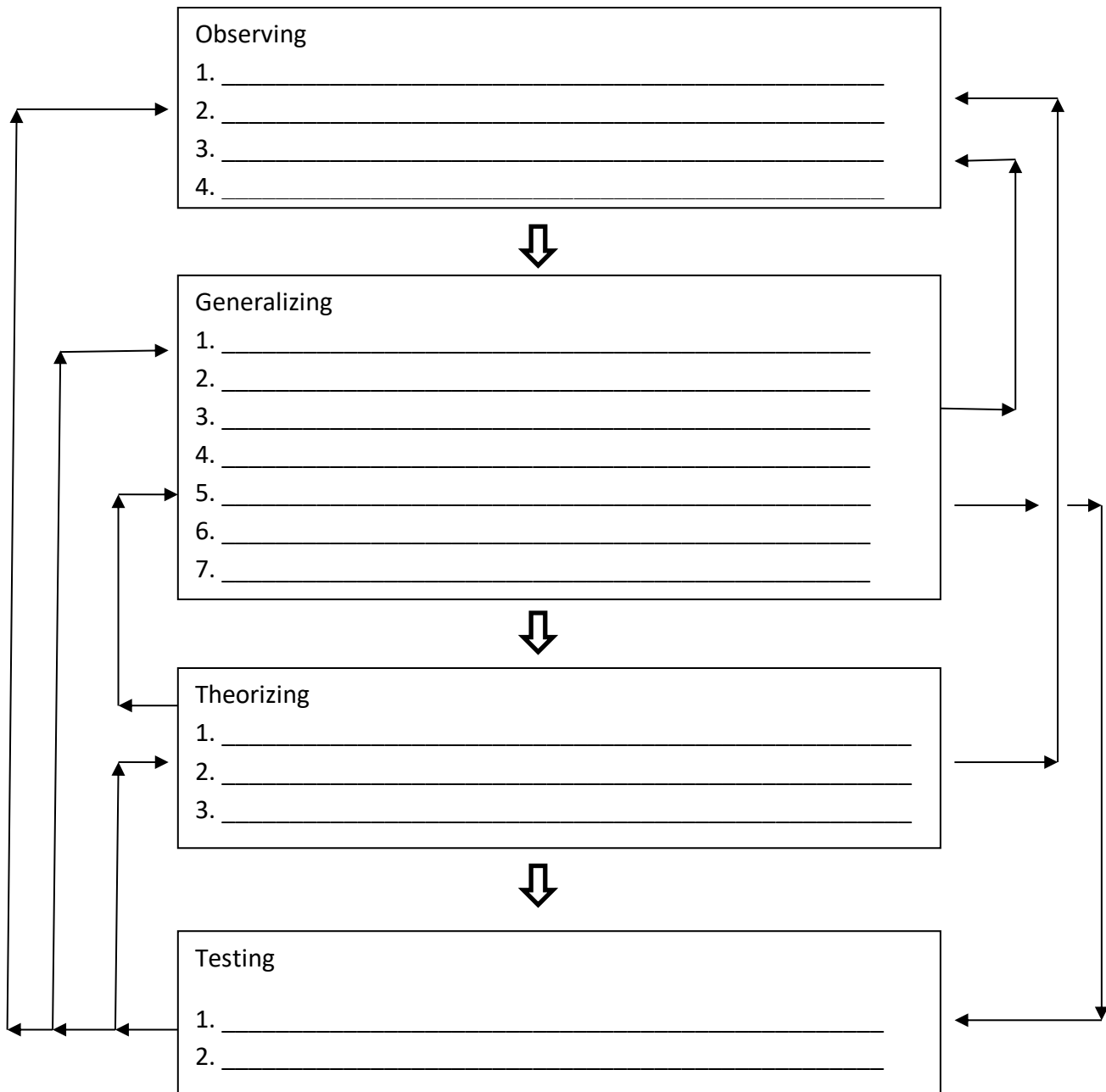
“ A scientific **theory** is a well- confirmed framework of ideas that explain what we observe.

A **model** is a theory that can be visualized, and a **principle** or **law** is one idea within a more general theory. The word *law* can be misleading because it sounds so certain. As we will see, scientific ideas are never absolutely certain.

“Note that a theory is a well-confirmed framework of ideas. It’s a misconception to think that a scientific theory is mere guesswork, as nonscientists occasionally do when they refer to some idea as ‘only a theory’. Some people who disliked Copernican theory [heliocentric system] argued that it was a ‘mere theory’ that need not be taken seriously. Today, people who dislike the theory of biological evolution attack it on similar grounds. Theories - well-confirmed explanations of what we observe – are what science is all about and are as certain as any idea can be in science.

“The correct word for a reasonable but unconfirmed scientific suggestion (or guess) is **hypothesis**. For example, Kepler’s first unconfirmed suggestion that the planets might move in elliptical orbits was a hypothesis. Once the data of Brahe and others confirmed Kepler’s suggestion, elliptical orbits took on the status of theory rather than mere hypothesis.”

Scientific Method Flow Chart



IMPORTANT:

"Communication": Common to _____ of the Scientific Method

Key Points in the lingo and protocol of science and the Scientific Method

1. Theory:

2. Hypothesis:

3. Idealizations (Galileo):

4. Limiting the Scope of Inquiry (Galileo):

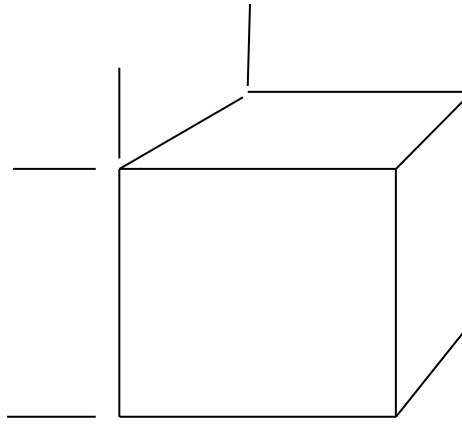
5. Quantitative methods (Galileo):

6. Creating a model:

7. Repeatable, predictable results/outcomes (Newton):

8. Fact-based rather than authority-based knowledge:

Volume:



Volume = length x height x width

$$= \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \underline{\hspace{2cm}}$$

and also = $\underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \underline{\hspace{2cm}}$

Therefore, $\underline{\hspace{2cm}} \text{ M}^3$ is equivalent to $\underline{\hspace{2cm}}$ or $\underline{\hspace{2cm}} \text{ cm}^3$

Additionally:

$$1 \text{ M}^3 = \underline{\hspace{2cm}} \text{ or } \underline{\hspace{2cm}} \text{ liters (L)}$$

$$1 \text{ liter} = \underline{\hspace{2cm}} \text{ or } \underline{\hspace{2cm}} \text{ milliliters (mL)}$$

Using “factor-labeling” conversion method to determine # mL in 1 M^3 :

$$\begin{array}{ccccccc} 1 \text{ M}^3 & \times & 10^3 \text{ Liters} & \times & 10^3 \text{ milliliters} & = & \underline{\hspace{2cm}} \text{ milliliters} \\ 1 & & 1 \text{ M}^3 & & 1 \text{ Liter} & & \end{array}$$

Since 1 M^3 equals $\underline{\hspace{2cm}} \text{ cm}^3$ and also $\underline{\hspace{2cm}} \text{ mL}$,

$\underline{\hspace{2cm}} \text{ cm}^3 = \underline{\hspace{2cm}} \text{ mL}$; a cm^3 is also referred to as a “ $\underline{\hspace{2cm}}$ ”

Mass Density Calculations

Mass Density (D_m) (also referred to simply as “density”)

is measured in _____ per _____ or ____/_____

Example 1:

Determine the D_m of a 67.5 gram sample of material with a volume of 30 cm³

Solution:

Use factor-labeling to convert grams/cm³ to Kilograms/M³

1. Restate the raw data as fraction:

$$\frac{67.5 \text{ grams}}{30 \text{ cm}^3}$$

2. Add conversion factors for cancellation:

$$\frac{67.5 \text{ grams}}{30 \text{ cm}^3} \times \frac{1 \text{ Kg}}{10^3 \text{ grams}} \times \frac{10^6 \cancel{10^3} \text{ cm}^3}{1 \text{ m}^3}$$

3. Restate with remaining terms and perform necessary calculations:

$$\frac{67.5 \times 10^3 \text{ Kg}}{30 \text{ m}^3} = \text{_____ Kg/m}^3$$

NOTE:

Determining the D_m of a material can serve as an indicator of the chemical identity of the material.

Example 2:**Predicting the mass of a sample of known material**

Given a 50 cm^3 sample of lead, predict the mass

Solution: Set up a proportionality equation using the known D_m of lead

Step 1:

State the known D_m of lead

$$\frac{11.3 \times 10^3 \text{ Kg}}{m^3}$$

Step 2:

Set up as equivalent to given sample

$$\frac{11.3 \times 10^3 \text{ Kg}}{m^3} = \frac{x \text{ g}}{50 \text{ cm}^3}$$

Step 3:

Convert all quantities to like terms (grams, cm^3 , since this is a small sample)

$$\frac{11.3 \times 10^6 \text{ g}}{10^6 \text{ cm}^3} = \frac{x \text{ g}}{50 \text{ cm}^3}$$

Step 4: Cross-multiply

$$\frac{11.3 \times 10^6 \text{ g}}{10^6 \text{ cm}^3} = \frac{x \text{ g}}{50 \text{ cm}^3}$$

Review: Cross-multiplying	
$\frac{a}{b} = \frac{c}{d}$ \downarrow $a \times d = b \times c$	$\frac{2}{3} = \frac{12}{18}$ \downarrow $2 \times 18 = 3 \times 12$

Now the equation becomes:

$$\underline{\hspace{2cm}} \times \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$$

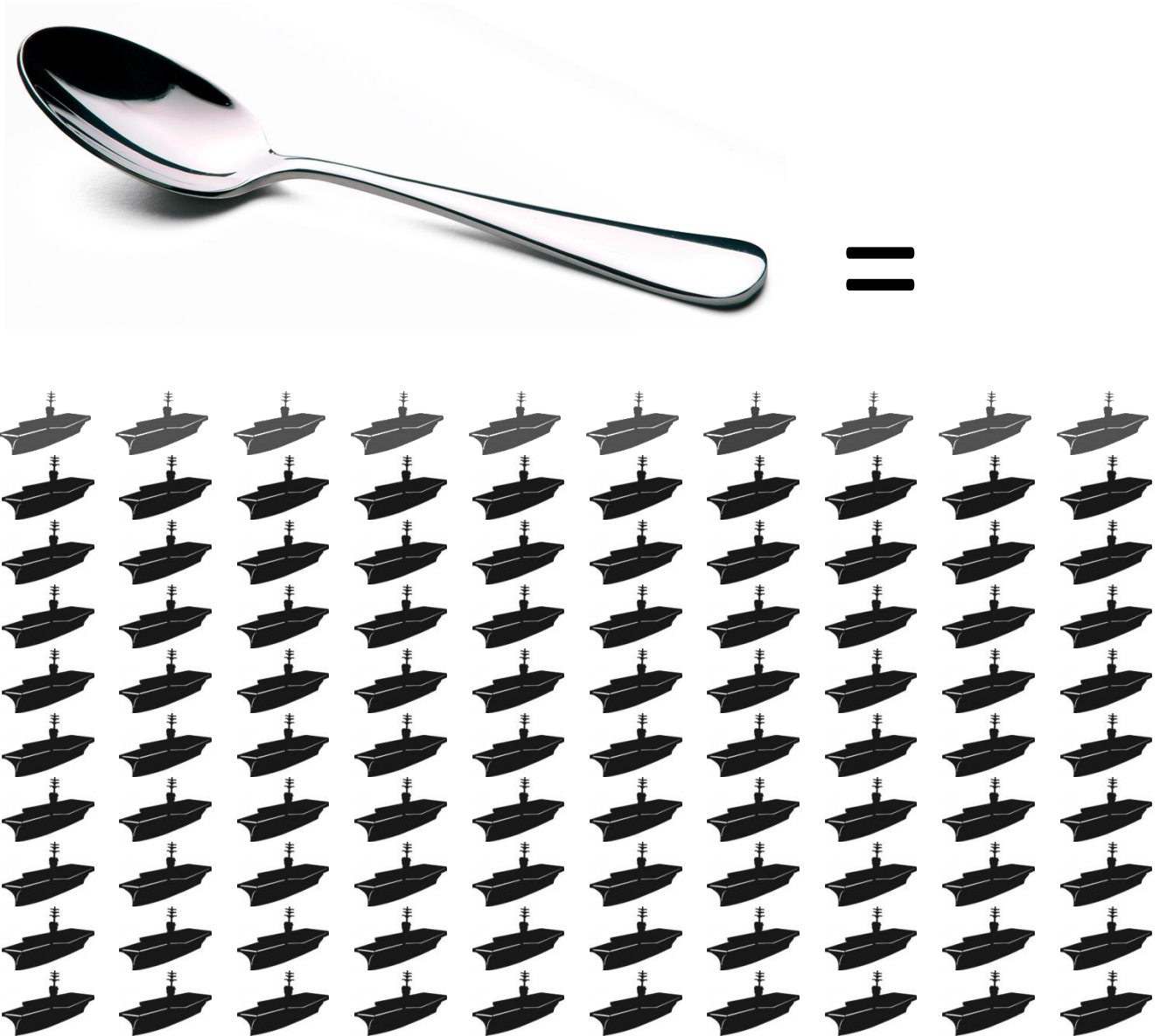
After canceling like terms, the equation becomes

$$\underline{\hspace{2cm}} \times \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$$

Thus, a 50 cm^3 sample of lead has a mass of grams

Neutron Stars: The ultimate in mass density:

If a star has sufficient mass (that is to say, 8 to 20 times more than our own Sun) when it goes _____, the atoms of the remaining material in the core are ripped apart by the extreme _____ and the extreme _____. During this process electrons combine with protons to form _____. Since the volume of a normal atom is over _____ empty space, this once-empty volume is now filled with neutrons. The result is a material so dense that a teaspoon of this substance can weigh _____, or the same as _____ aircraft carriers.



Self check:

Determine the D_m of a 273 gram sample of material with a volume of 35 mL	answer:
Determine the mass of a 95 cm^3 sample of iron	answer:

Vectors:

Two types of measurement used in Physics; they are

1. _____ measures

b. Indicate _____ only

2. _____ measures

a. Indicate _____ and _____

Examples:

Scalar

Vector

Since vector measures include the component of _____ then that component must be taken into consideration during _____ .

Example 1: Two bungee cords pulling in opposite directions:

Example 1a:



Net force: _____

Example 1b:



Net force: _____

Example 2: Two bungee cords pulling in the same direction:



Net force: _____

Note:

At this point you should see the _____ of net forces, or

the “ _____ - _____ ”

Example 3: Two bungee cords pulling at a 90° angle relative to one another



Solution: Use “_____ to _____” schematic

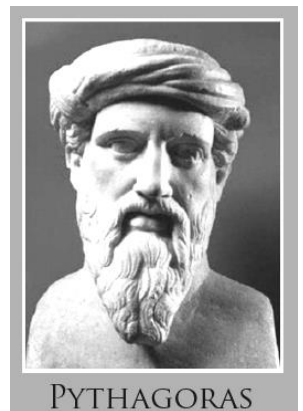


The sum of these two vectors is called a “_____”

BUT,

The Pythagorean Theorem will solve _____ only

What about direction?

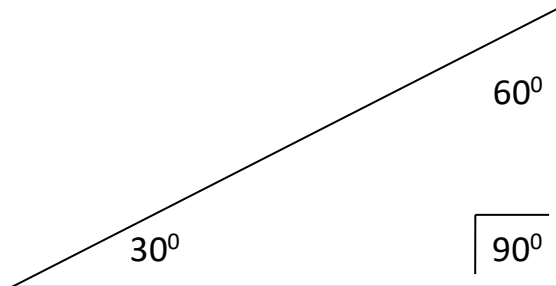


PYTHAGORAS

Basic Right-Angle Trigonometry

(Invented by _____)

Given: a 30-60- 90 triangle



One of the unique characteristics of a 30-60-90 triangle is that

the side _____ the 30° angle

is always _____ - _____ the length of the _____.

In other words, given the _____ angle,

the _____ of the _____ side over the _____

will always be _____ - _____, or _____.

In Right-Angle Trigonometry, this ratio is called

the _____ of the _____

Thus, we can state that the “_____ of 30° is _____”

Trig on a calculator:

Depending on what model calculator you are using, you will do trig functions in one of two ways. We will use the **Sine (sin) of 30°** as an example.

Method 1:

1. Hit
2. enter "30"
3. Hit "="
4. **Your answer should be "0.5."**
5. **If not**, you're probably in "**radian mode**" and using a graphing calculator.
6. Go to (you may need to use "**shift**" or "**2nd**" to get there)
7. You should see a screen showing both "**degree**" and "**radian.**"
8. Select "**degree**"
9.
10.
11. Repeat steps 1 -3, your answer should now be "**0.5**"

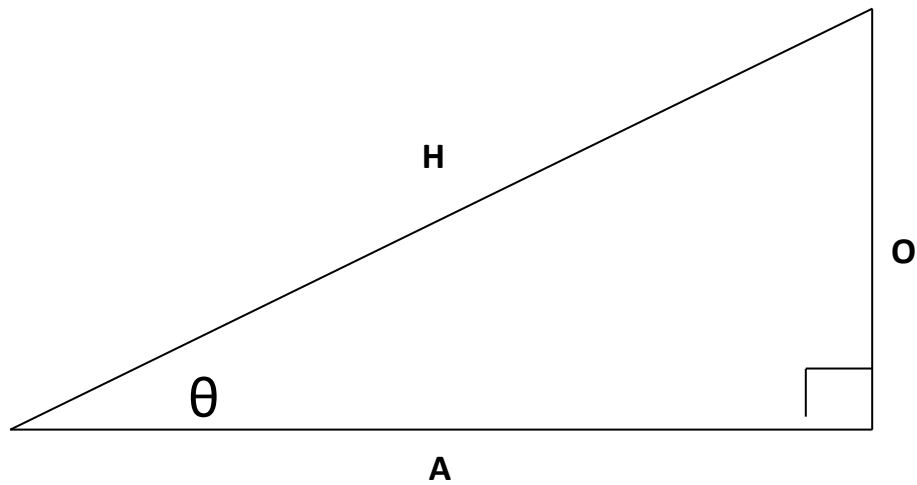
Method 2 (more common on simpler, less expensive calculators):

1. Enter "30"
2. Hit
3. Your answer should be "**0.5**"

Practice using other trig functions:

$$\text{Cosine } 30^{\circ} = .866$$

$$\text{Tangent } 30^{\circ} = .577$$



θ ("Theta"): _____

Hypotenuse: _____

Opposite: _____

Adjacent: _____

Sine θ ($\sin \theta$):

the ratio of the _____ side over the _____

Cosine θ ($\cos \theta$):

the ratio of the _____ side over the _____

Tangent θ ($\tan \theta$)

the ratio of the _____ side over the _____ side

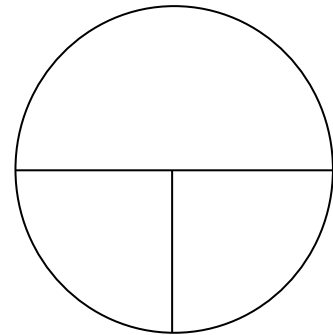
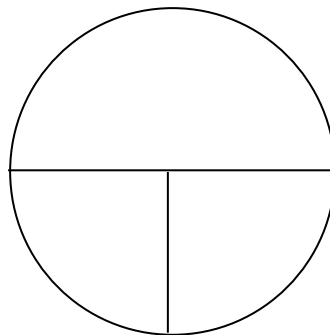
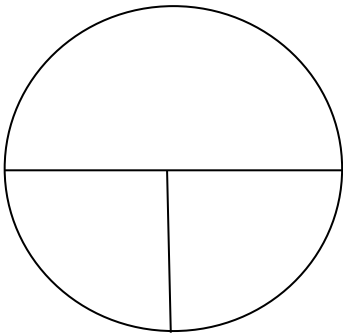
Stated more simply:

$$\sin \theta = \frac{O}{H}$$

$$\cos \theta = \frac{A}{H}$$

$$\tan \theta = \frac{O}{A}$$

Stated yet another way:



Sin θ =

O =

H =

Cos θ =

A =

H =

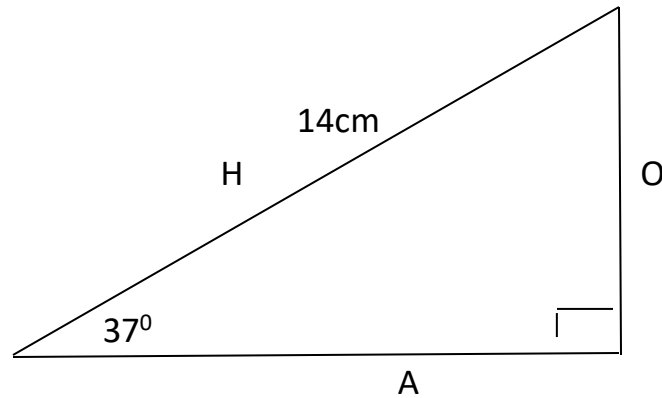
Tan θ =

O =

A =

Using Trig

Example 1.



Determine the lengths of sides "O" and "A"

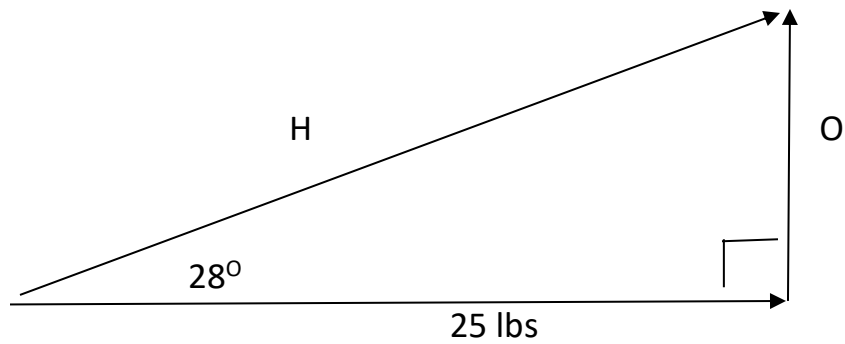
1. To determine "O" use "Sin", which uses the **known angle** and the **known hypotenuse (H)**

$$\begin{aligned} O &= (\text{Sin } 37^\circ) \times H \\ &= (\quad) \times (14) \\ &= \underline{\hspace{2cm}} \end{aligned}$$

2. To determine "A" use "Cos", which uses the **known angle** and the **known hypotenuse (H)**

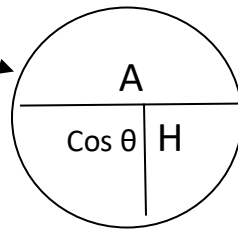
$$\begin{aligned} A &= (\text{Cos } 37^\circ) \times H \\ &= (\quad) \times (14) \\ &= \underline{\hspace{2cm}} \end{aligned}$$

Example 2.



Determine the lengths of sides "H" and "O"

1. To determine "H" use "Cos", which uses the **known angle** and the **known adjacent (A)**

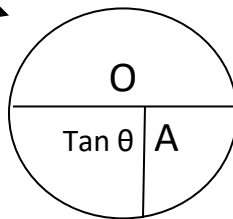


$$H = \frac{A}{\text{Cos } 28^\circ}$$

$$= \frac{25}{\quad}$$

= _____

2. To determine "O" use "Tan", which uses the **known angle** and the **known adjacent (A)**

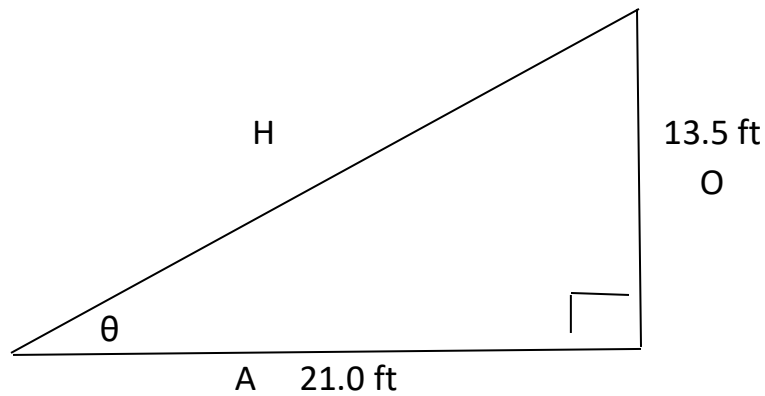


$$O = (\text{Tan } 28^\circ) \times A$$

$$= (\quad) \times (25)$$

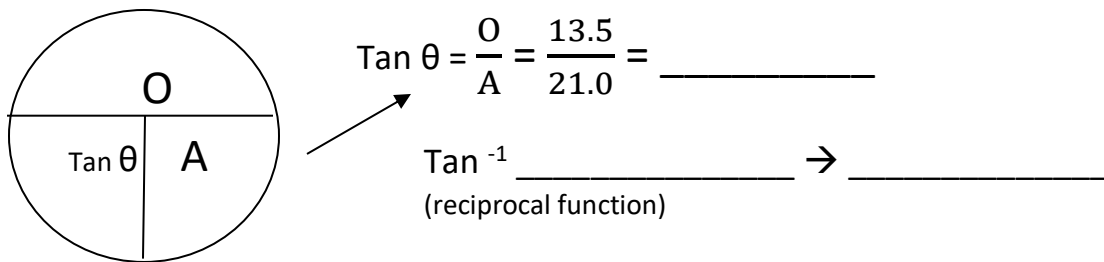
= _____

Example 3:



Determine length of “H” and the value of “θ”

1. Begin by determining “θ”. Since “O” and “A” are known, use “Tan”.



2. Determine “H” by using either **Sine** or **Cosine**

$$H = \frac{O}{\sin \theta}$$

$$H = \frac{A}{\cos \theta}$$

Using the “**reciprocal function**” on the calculator

Since we know that the **Sine of 30° is 0.5**, we’ll start there.

Method 1:

1. Hit “**Shift**” or “**2nd**”
2. Hit
3. Enter “.5”
4. Hit “=”
5. Your answer should be “**30**”

Method 2 (for simpler, less expensive calculators):

1. Enter “.5”
2. Hit “**Shift**” or “**2nd**”
3. Hit
4. Your answer should be “**30**”

**Practice using other trig
functions:**

$$\cos^{-1} .866 \rightarrow 30^\circ$$

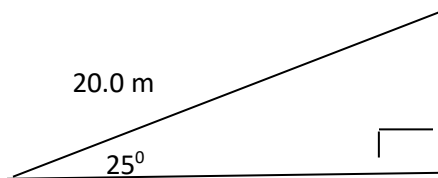
$$\tan^{-1} .577 \rightarrow 30^\circ$$

Informal Lab: Practice problems

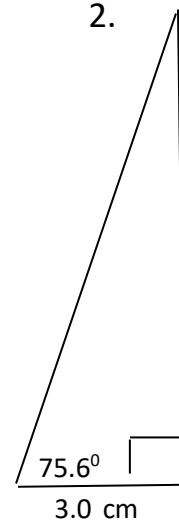
ASSIGNMENT: Solve for unknown sides and angles using trigonometry
plus additional instructions below:

1. Do **NOT** Pythagorean Theorem!
2. **DRAW** these in larger scale on a separate paper – use a straight-edge if it helps.
 The idea is to get you used to drawing, *as Galileo recommends!*

1.

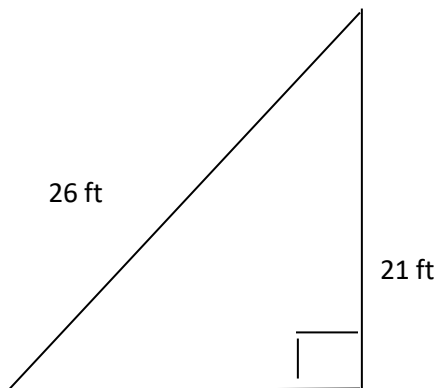


2.

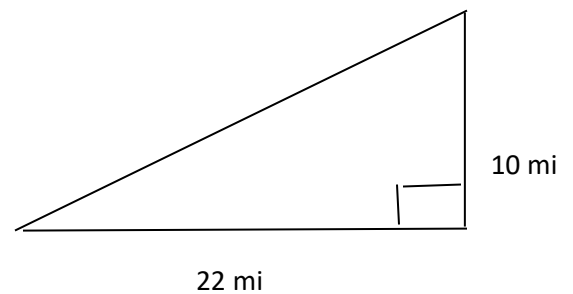


Hint:
 Do **not**
 “rotate”
 this one!

3.



4.



Practical principles:

1. The sine, cosine, and tangent of any/every angle between _____ and _____ is _____ to that angle alone.
2. Thus, if we know the sine, cosine and/or tangent of an angle, then we have the means to _____ the original angle.
3. NOTE:
This course will take the “old-school trig” approach in analyzing angles, and therefore all angles (“vectors”) will be evaluated as if their measures are between _____ and _____ .

Example 1:

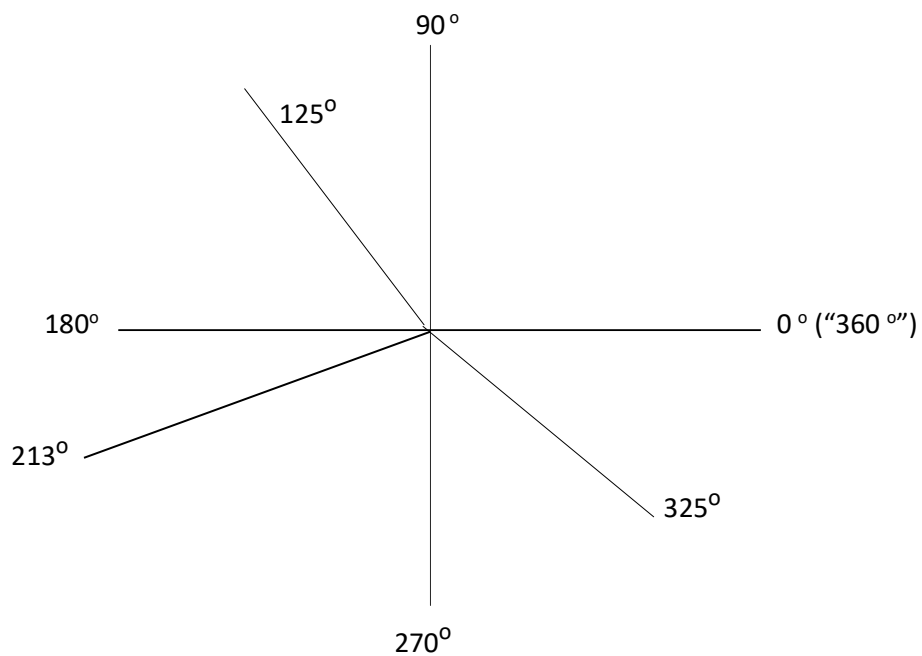
125° will be evaluated as _____ ($180^\circ - 125^\circ$) (measure from x-axis)

Example 2:

213° will be evaluated as _____ ($213^\circ - 180^\circ$) (measure from x-axis)

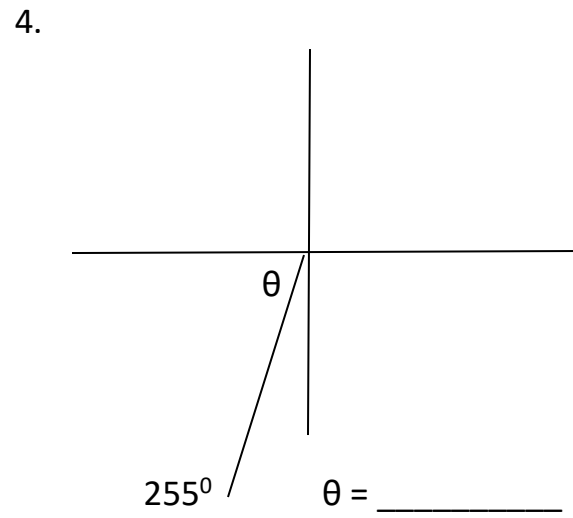
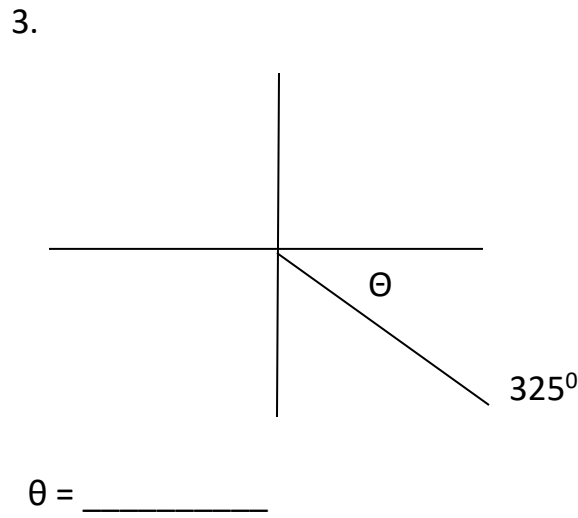
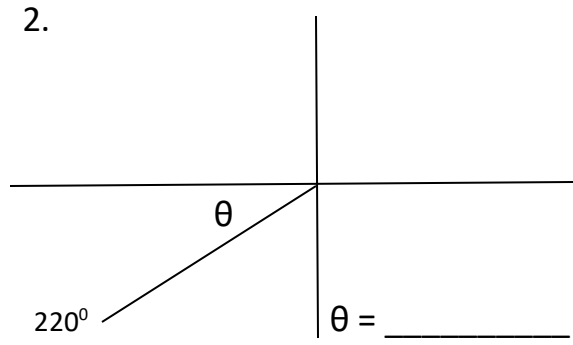
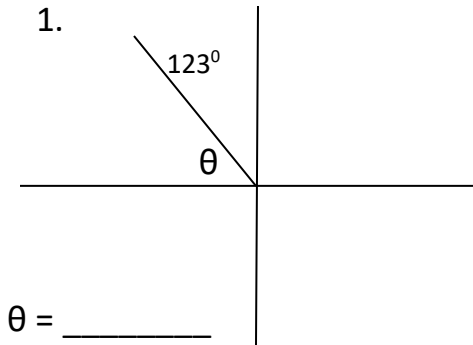
Example 3:

325° will be evaluated as _____ ($360^\circ - 325^\circ$) (measure from x-axis)



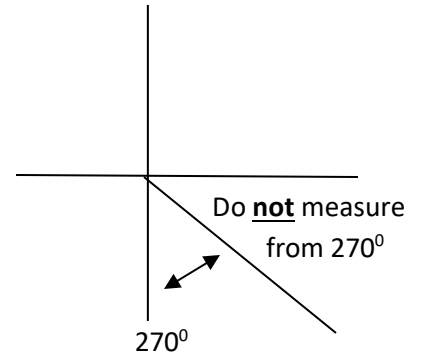
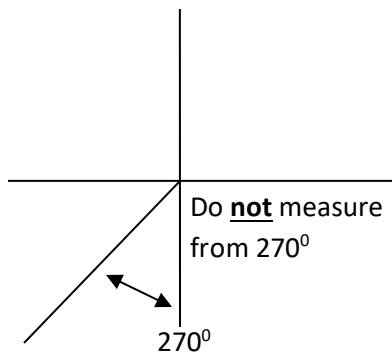
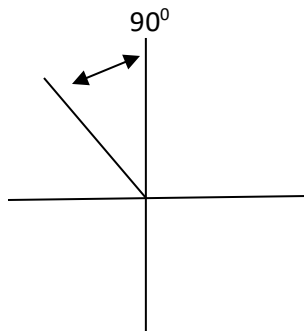
Informal Lab: Practice evaluating angles

Hint: **Always** measure from the closest horizontal ("x - axis")



Common mistakes:

Do not measure from



ANSWERS: 1. 57° ($180 - 123$) 2. 40° ($220 - 180$) 3. 35° ($360 - 325$) 4. 75° ($255 - 180$)

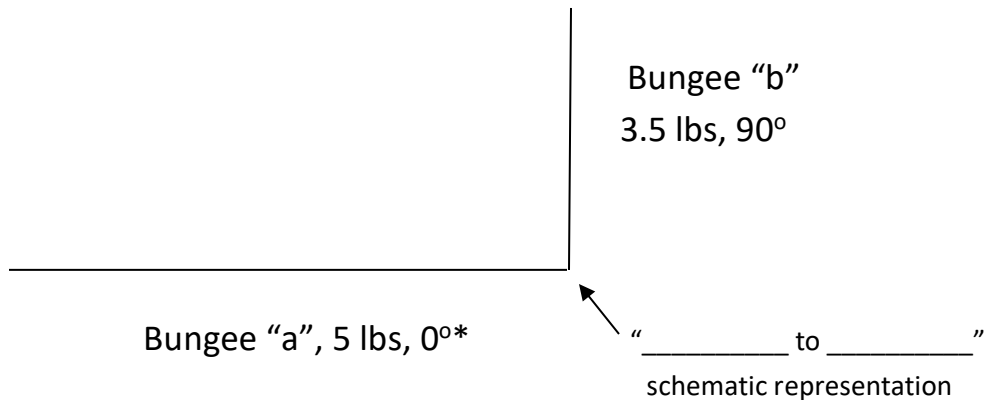
Back to the beginning of this topic:

Given:

1. Two bungee cords attached at a common point.
2. Bungee "a" pulls with 5 pounds of force at 0°
3. Bungee "b" pulls with 3.5 pounds of force at 90°
4. What is the sum of the forces of the two bungee cords?

Solution:

Draw *:



*** NOTE: Always draw _____ vector first beginning with the _____**

1. Calculate the tangent of the unknown angle "____" : $\tan = \frac{\text{_____}}{\text{_____}} = \text{_____}$
2. \tan^{-1} _____ \rightarrow _____
3. Calculate the hypotenuse (or "_____")

Using trig, we know that $H = \frac{O}{\sin \theta}$ and/or $\frac{A}{\cos \theta}$

Selecting the first trig formula,

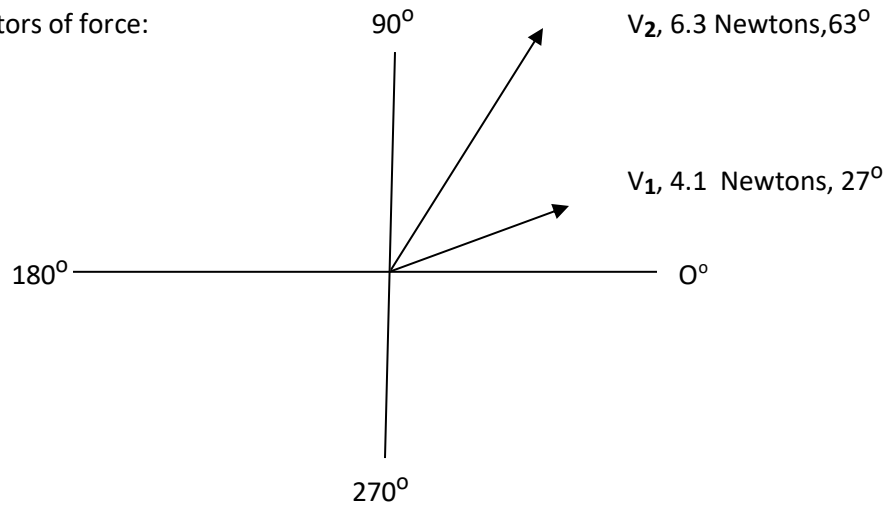
$H = \text{_____} = \text{_____} = \text{_____}$ (solution)

Thus, the sum (_____) of the forces of the two bungee cords is _____ at _____ degrees

Adding Vectors:

Example 1:

Given the following
vectors of force:

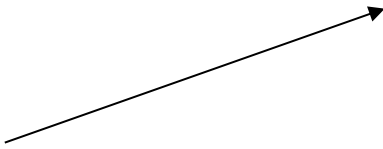


Determine the sum of $V_1 + V_2$

Solution:

- ① Draw each vector individually, and label accordingly
- ② Add component vectors and label accordingly
- ③ Use trig to solve for components
- ④ Add components
- ⑤ Construct new vector (“resultant”) using component sums
- ⑥ Use trig to evaluate resultant

V₁, 4.1 Newtons, 27°



$$A_1 = (\quad)x(\quad)$$

$$= \quad x \quad$$

$$= \quad$$

$$A_2 = (\quad)x(\quad)$$

$$= \quad x \quad$$

$$= \quad$$

$$O_1 = (\quad)x(\quad)$$

$$= \quad x \quad$$

$$= \quad$$

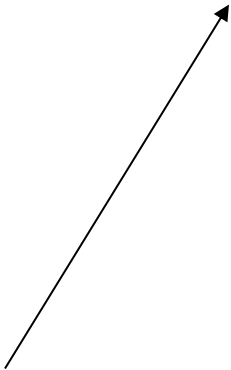
$$O_2 = (\quad)x(\quad)$$

$$= \quad x \quad$$

$$= \quad$$

A ₁ _____	O ₁ _____
+A ₂ _____	+ O ₂ _____
A total	O total

V₂, 6.3 Newtons, 63°

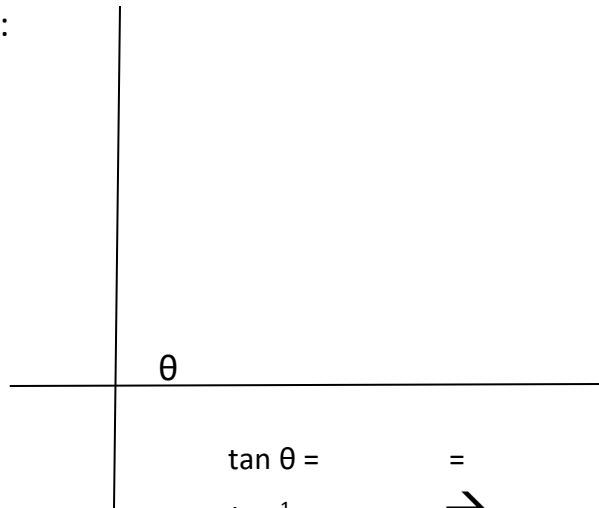


Construct/draw in order:

A total

O total

Resultant

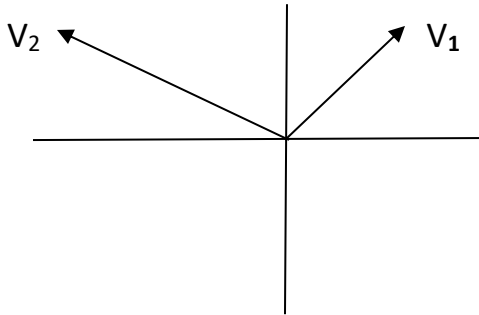


$$\tan \theta = \quad = \quad = \quad$$

$$\tan^{-1} \quad \rightarrow \quad$$

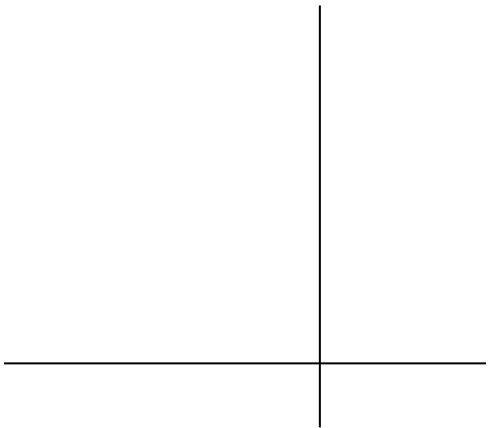
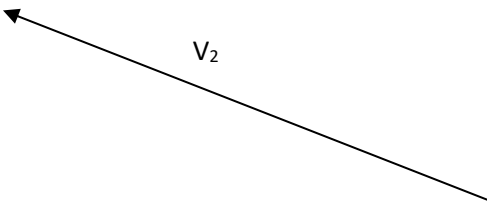
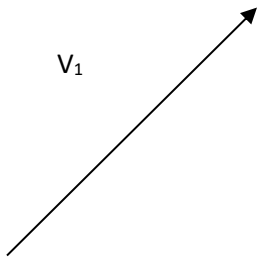
Resultant (H) = _____ = _____ = _____

Example 2:

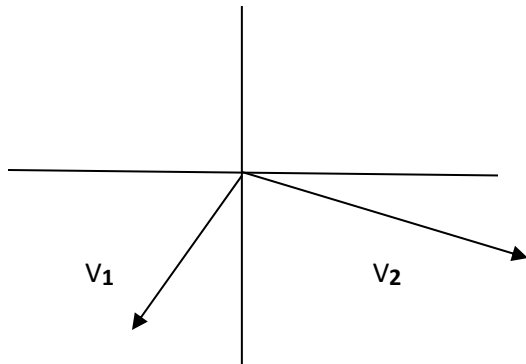


$V_1: 48^\circ, 50 \text{ meters/sec}$
 $V_2: 147^\circ, 75 \text{ meters/sec}$

A_1	O_1
A_2	O_2
A_t	O_t



Example 3:



$V_1: 245^\circ, 36 \text{ N}$

$V_2: 337^\circ, 68 \text{ N}$

A_1

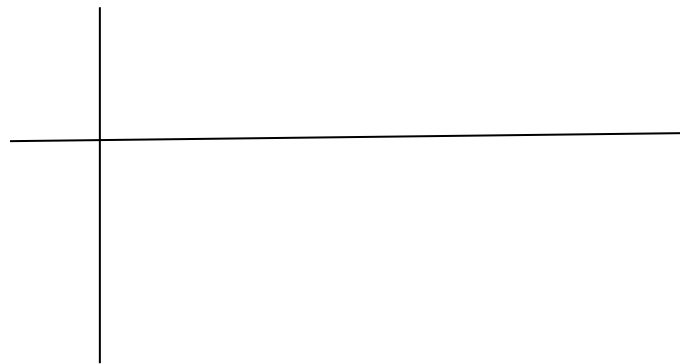
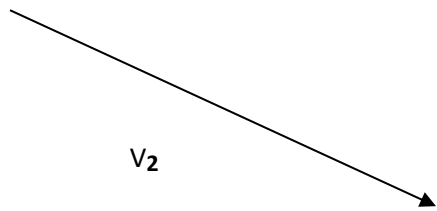
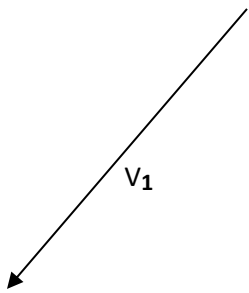
O_1

A_2

O_2

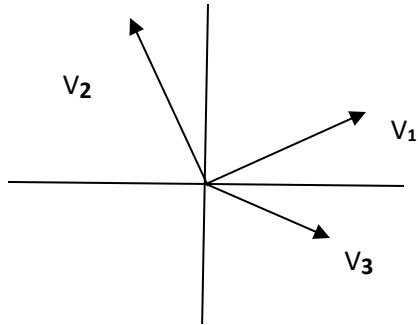
A_t

O_t



Forces in Equilibrium

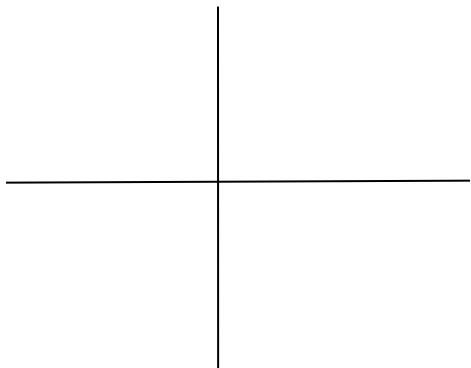
Given:



V₁

V₂

V₃



V₁ : 33°, 3.1 N

V₂ : 103°, 2.0 N

V₃ : 338°, 1.6 N

Calculations:

A₁

O₁

A₂

O₂

A₃

O₃

A_t

O_t

Resultant calculations:

Tan θ _____

Tan⁻¹ _____ = _____

$H = \frac{O}{\sin \theta} = \text{_____} = \text{_____}$

Calculate the vector that will cancel the resultant Equilibrium Vector (V_{eq}) calculations

Note: What is the sum of all component force vectors in a system in equilibrium?

MOTION

1. Velocity:

a. _____ measurement

b. _____ and _____

c. _____ over _____ ()

d. Measured in:

1. _____ per _____ (____/ ____) (British)

2. _____ per _____ (____/ ____) (Metric)

2. Average Velocity (V_{avg})

Averages _____ in velocity over a given period of time.

Example: Driving from Portland to Boston

3. Uniform Velocity:

Velocity that does not _____

(Example: " _____ - _____ ")

—

4. Acceleration:

a. _____ measurement

b. A _____ in _____ * over _____

* ("V_Δ" or " _____ V ")

("Δ" = " _____ ")

c. Measured in:

1. _____ per _____ per _____ (____ / ____)
(British)

2. _____ per _____ per _____ (____ / ____)
(Metric)

Explanation of units of Acceleration:

("ft/sec² = feet per second per second")

("m/sec² = meters per second per second")

Acceleration (continued):

1. The acceleration of gravity (a_g)

On Earth:

a. _____ ft/sec² (British)

b. _____ m/sec² (Metric)

c. Thus, one "g" = _____ or _____

CAUTION:
Gravity is acceleration,
BUT
Not all acceleration is
gravity!

2. Key words:

a. "Boost":

b. "Retro-burn"

c. Negative g's



3. Acceleration due to a change in direction:

Since acceleration is defined as

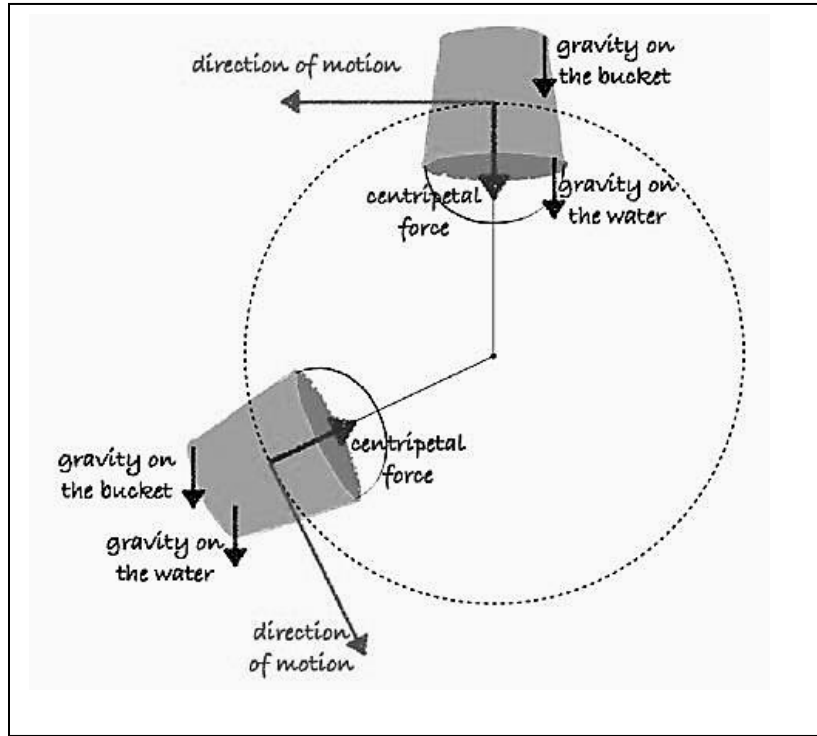
a _____ in _____ ,

and velocity is defined as

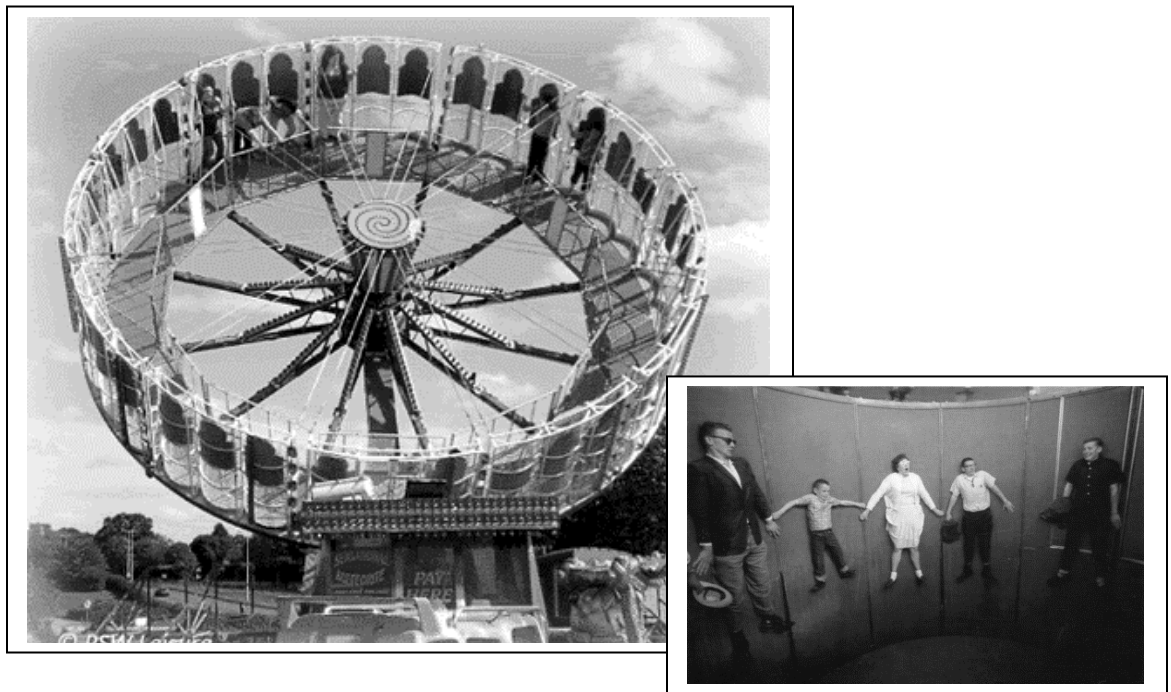
_____ and _____ ,

then a _____ in _____ results in _____.

Example 1: Beach Bucket



Example 2: The "Gravitron"



Critical Factors in Acceleration Calculations:

1. V_i :

2. V_f :

3. a :

4. s :

5. t :

“ Three outa five ain’t bad!”

Given any _____ of the above factors,
the remaining _____ factors may be calculated

Basic Formulas Used in Acceleration Problems:

V_i	V_f	a	s	t	basic formula:

Acceleration Formula Cheat Sheet

$t = \otimes$			
$a = \frac{V_f^2 - V_i^2}{2s}$	$s = \frac{V_f^2 - V_i^2}{2a}$	$V_f = \sqrt{V_i^2 + 2as}$	$V_i = \sqrt{2as - V_f^2}$
$s = \otimes$			
$V_f = at + V_i$	$V_i = V_f - at$	$a = \frac{V_f - V_i}{t}$	$t = \frac{V_f - V_i}{a}$
$a = \otimes$			
$s = .5(V_f + V_i)t$	$t = \frac{s}{.5(V_f + V_i)}$	$V_f = \frac{s}{.5t} - V_i$	$V_i = \frac{s}{.5t} - V_f$
$V_f = \otimes \quad V_i = 0$			
$s = .5at^2$	$a = \frac{s}{.5t^2}$	$t = \sqrt{\frac{s}{.5a}}$	
$V_f = \otimes \quad V_i \neq 0$			
$s = V_i t + .5at^2$	$t = \frac{-V_i \pm \sqrt{V_i^2 + 2as}}{a}$	$v_i = \frac{.5at^2}{t}$	$a = \frac{s - v_i t}{.5t^2}$

Points to ponder

Given this formula: $s = V_i t + \frac{1}{2} at^2$

Solve for t

- ① $s = V_i t + .5at^2$
- ② $V_i t + .5at^2 = s$
- ③ $\quad +(-s) \quad +(-s)$
- ④ $V_i t + .5at^2 + (-s) = 0$
- ⑤ $.5at^2 + V_i t + (-s) = 0$

⑥

⑥

Change symbol from to	

Informal Lab: Working through acceleration problems

Example 1:

How long will it take an object to drop 4 feet?

①

②

③

Step 1: Does this question involve gravity and /or acceleration? If so, then go to:

Step 2: Inventory

② V_i V_f ② a ③ s ① t 

Step 3: What is the question?

Step 4: **Look for the “odd man out” (⊗)**Step 5: **Look for ⊗ on the Cheat Sheet**

Step 6: Select formula corresponding to “?”

Step 7: Insert correct values in formula and solve

- **Be sure to use correct standard units! Convert if necessary.**

Example 2:

(Part 1)

A rock is dropped from a bridge. It takes 1.35 seconds for the rock to strike the water below. How high (in ft) is the bridge above the water?

V_i

V_f

a

s

t

(Part 2)

How fast is the rock travelling at impact?

V_i

V_f

a

s

t

Example 3.

A ball is thrown straight down from a cliff. The velocity of the ball as it leaves the thrower's hand is 60 ft/sec. How far will the ball have travelled after 2 sec.?

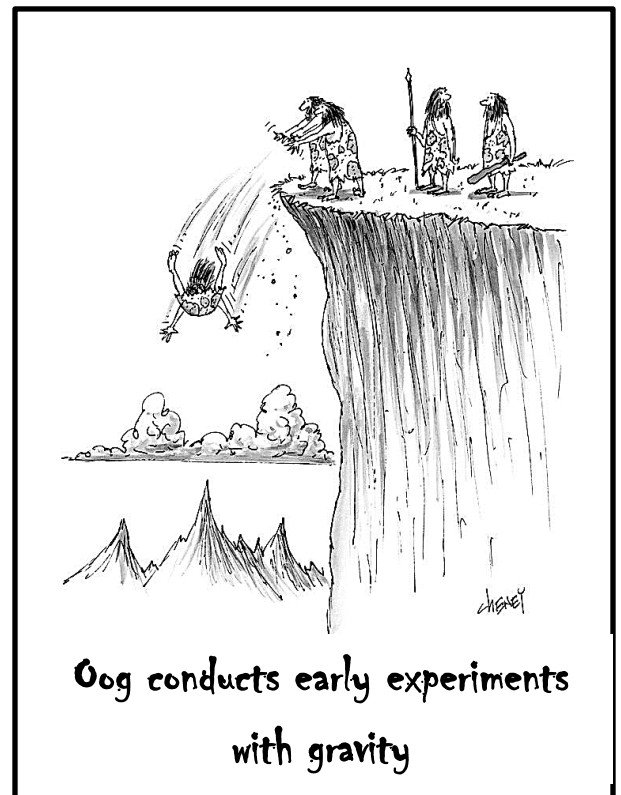
V_i

V_f

a

s

t



Example 4.

A rocket boosts from the launch pad at 48 ft/sec^2 . How high is the rocket after 5 sec.?



Example 5.

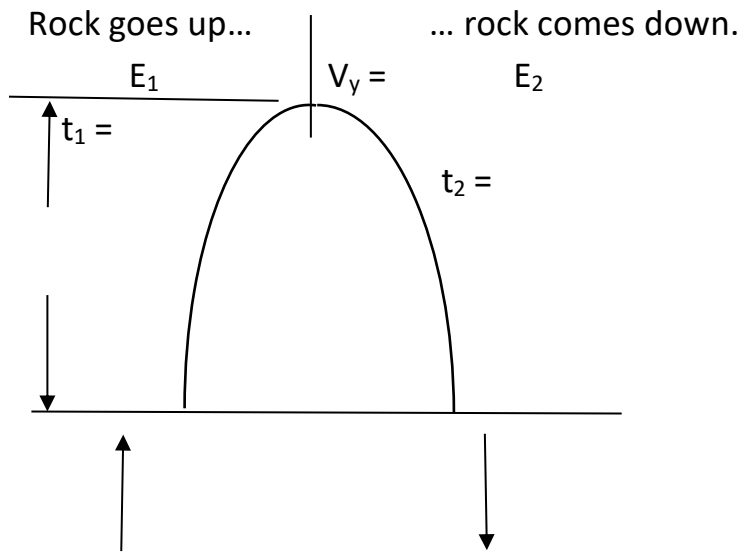
A car goes from 55MPH to 70 MPH in 10 sec. What is its rate of acceleration?

(Hint: convert to standard units **first**)

Example 6.

An aircraft with a landing speed of 180 MPH lands on an aircraft carrier by catching the arresting wire and coming to a complete stop in 2 sec. How many G's does the pilot experience? **(Be sure to convert to correct units first!)**





"You know, I used to like this hobby. ... But shoot! Seems like everybody's got a rock collection."

<p>Q1: What is the initial velocity (V_i) of the rock going up?</p> <p>V_i V_f a s t</p> <p style="text-align: right;">$V_i =$</p>	<p>Q2: How long does it take the rock to reach max height?</p> <p>V_i V_f a s t</p> <p style="text-align: right;">$t =$</p>
<p>Q3: How long does it take the rock to come back down?</p> <p>V_i V_f a s t</p> <p style="text-align: right;">$t =$</p>	<p>Q4: What is the final velocity of the rock at the return point?</p> <p>V_i V_f a s t</p> <p style="text-align: right;">$V_f =$</p>

Informal Lab Problems:

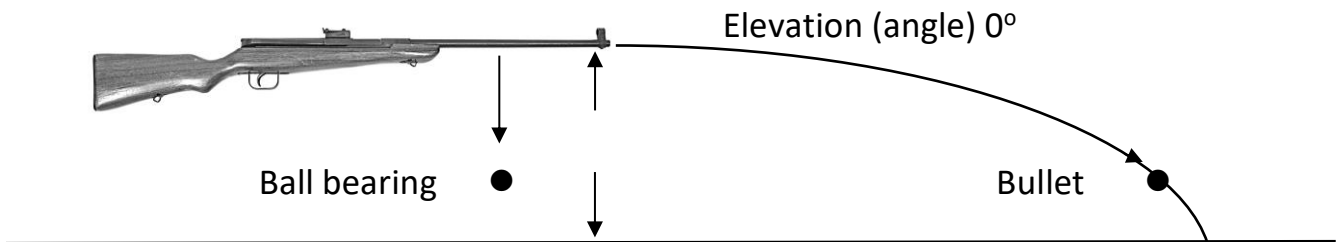
1. A bullet is fired vertically with an initial velocity of 250 m/sec.
Discounting air resistance,
 - a. How high does it go?
 - b. How long does it take to reach max height?



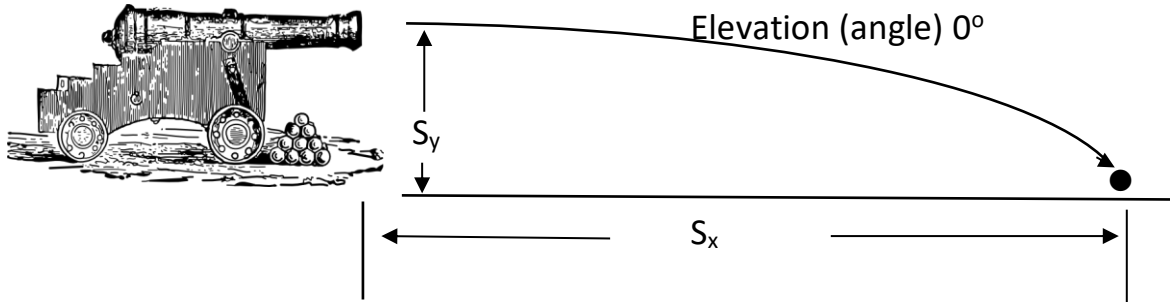
2. A bullet is fired vertically and reaches a max height of 700 ft
Discounting air resistance,
 - a. What is its initial velocity?
 - b. How long does it take to reach max height?

Kinematics: Motion in Two Dimensions

Example 1:



Example 2:



Using a level shot to determine Muzzle Velocity (V_{muzzle})

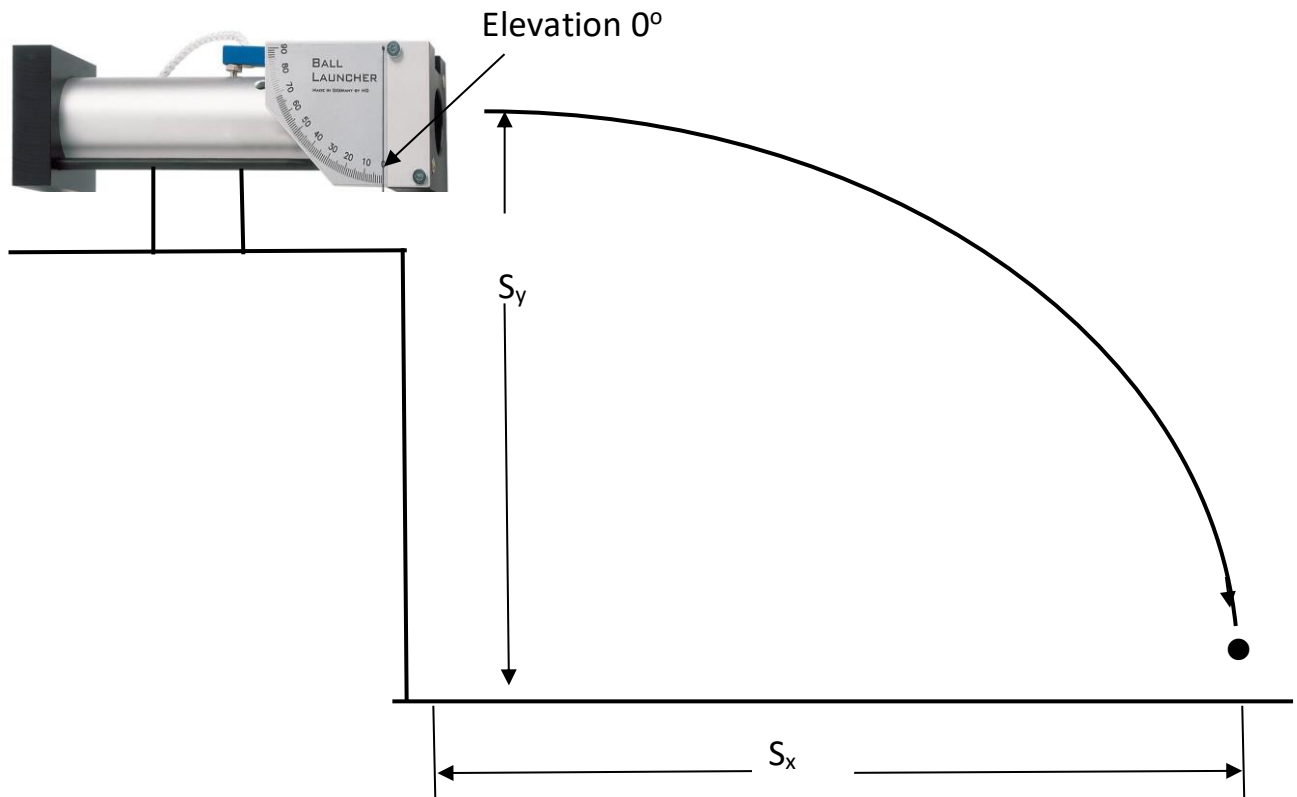
Theory:

1. Definition of velocity: (—)
2. V_x is stipulated as _____ (“idealization”)
3. V_{muzzle} is set at 0° elevation and is therefore _____ to V_x
4. “S” is measured as _____
5. “t” is calculated using _____

Calculations/measurements:

1. S_x _____
2. S_y _____
3. $t =$ _____
4. $V_{\text{muzzle}} =$ _____

Determining Muzzle Velocity



$$S_y = \text{_____} \text{ (as measured)}$$

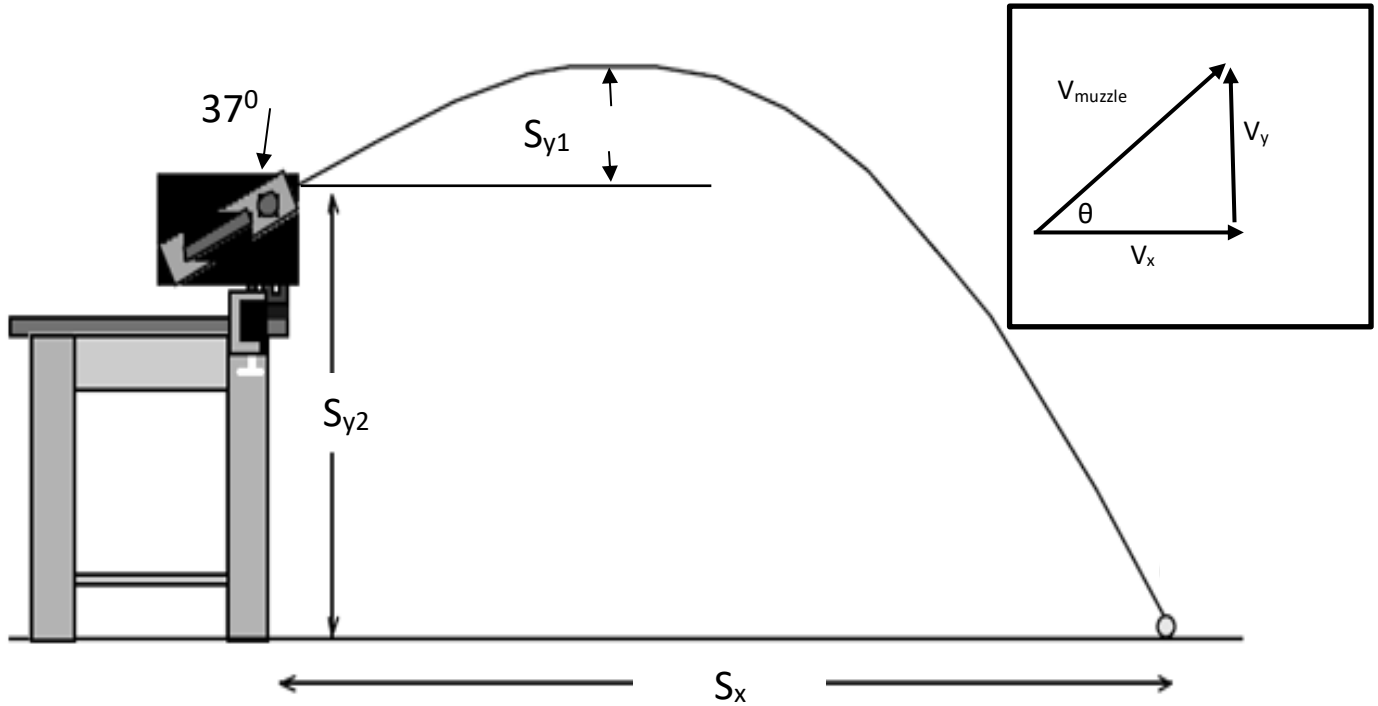
$$S_x = \text{_____} \text{ (as measured)}$$

$$t = \sqrt{\frac{S_y}{.5a}} = \sqrt{\frac{\text{_____}}{.5a}} = \sqrt{\text{_____}} = \text{_____}$$

$$V_x = \frac{S_x}{t} = \frac{\text{_____}}{\text{_____}} = \text{_____} V_{\text{muzzle}}$$

(only when elevation is set at 0°)

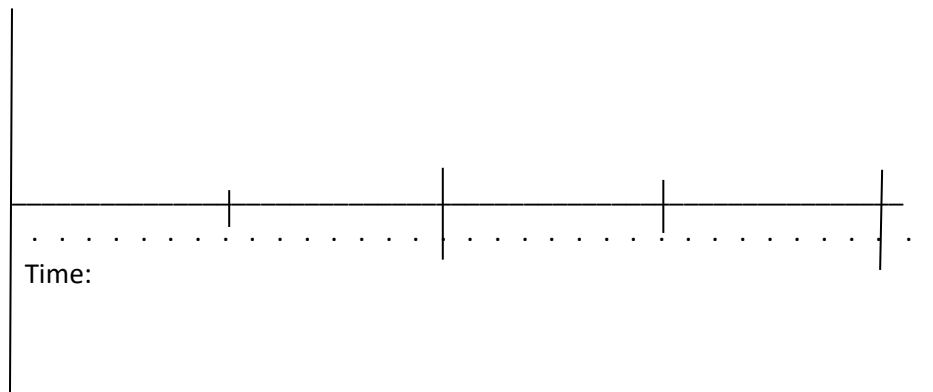
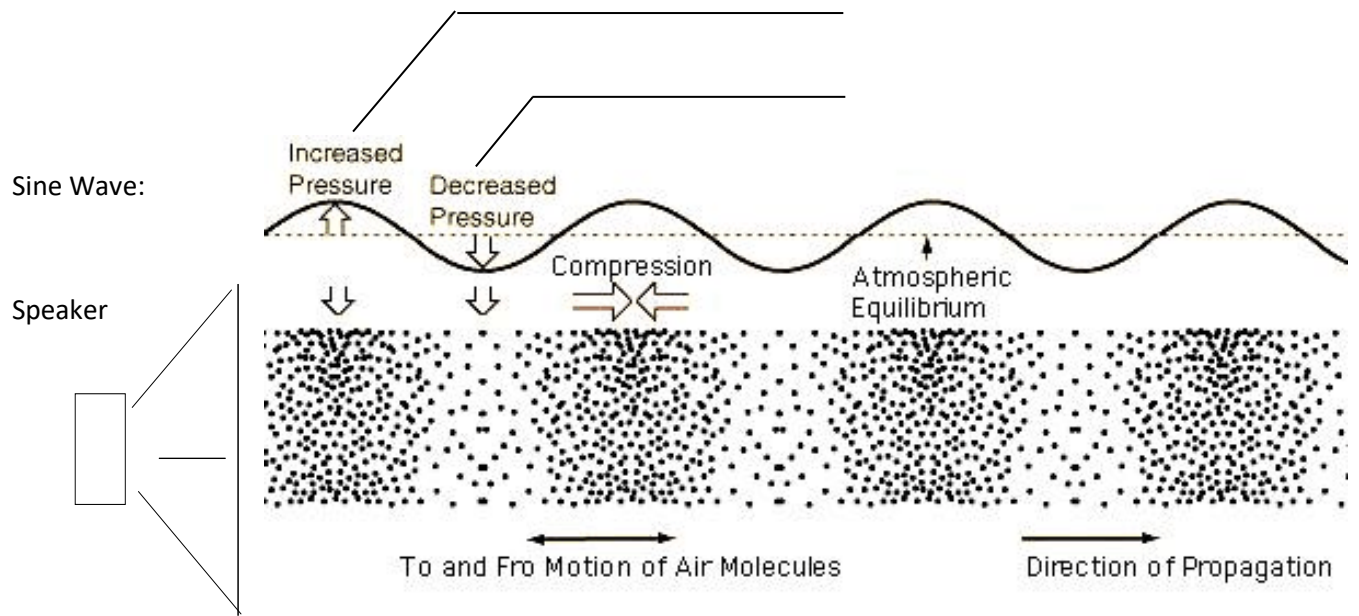
Predicting range of angled shot based on known V_m



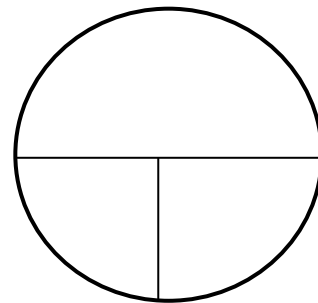
OBJECTIVE: Predict S_x given known V_{muzzle}

<p>1. Proposition: $S_x = \frac{V_x}{1} \times t_{total}, \longrightarrow (t_{total} = [(t_1) + (t_2)])$</p> <p>$= (\quad) \times [(\quad) + (\quad)] = \underline{\hspace{2cm}}$</p>	
3. $V_x =$	4. $V_y =$
5. $t_1 =$	6. $S_{y1} =$
6. $T_2 =$	

Sound:



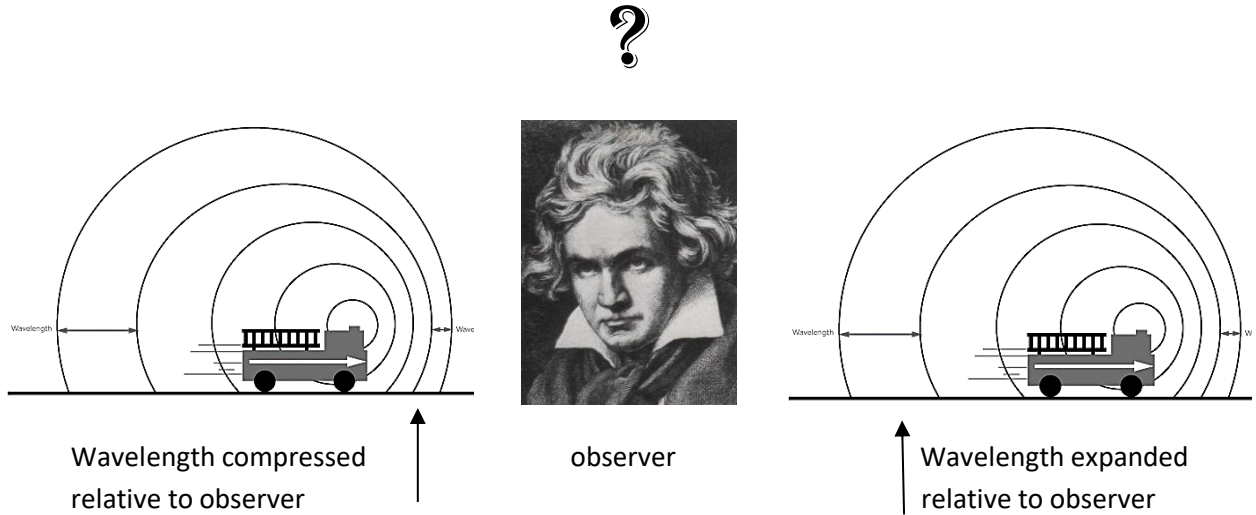
Frequency, wavelength, velocity:



The role of the medium in a mechanical wave

The medium determines _____ of a wave

The Doppler Effect:



Longer _____ = lower _____
 Shorter _____ = higher _____

Doppler equation: $f' = f \left(\frac{v}{v \pm v_s} \right)$

Where:

- v_s = Velocity of the Source
- v = Velocity of wave
- f = Real frequency
- f' = Apparent frequency

Equation to determine velocity of source:

$$V_s = \frac{V (f' - f)}{f'}$$

Doppler Effect Real World Example:

A sonar analyst detects an underwater sound at a frequency of 319.63 HZ.

He knows from prior intelligence that sound is actually propagated at 318.00 hz.

1. Is the sound source approaching or receding?
2. What is the speed of the source in Knots (nautical miles per hour)?

Data:

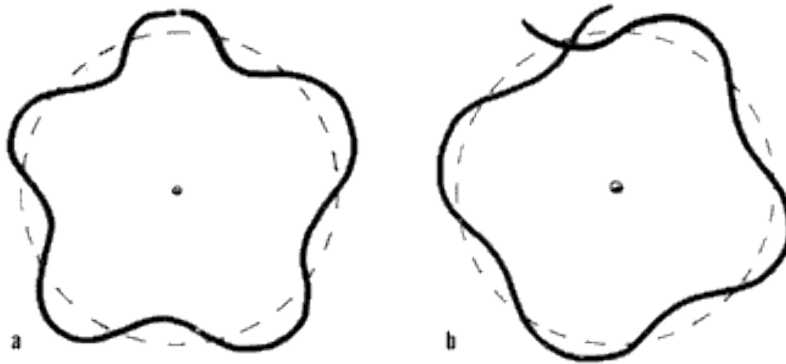
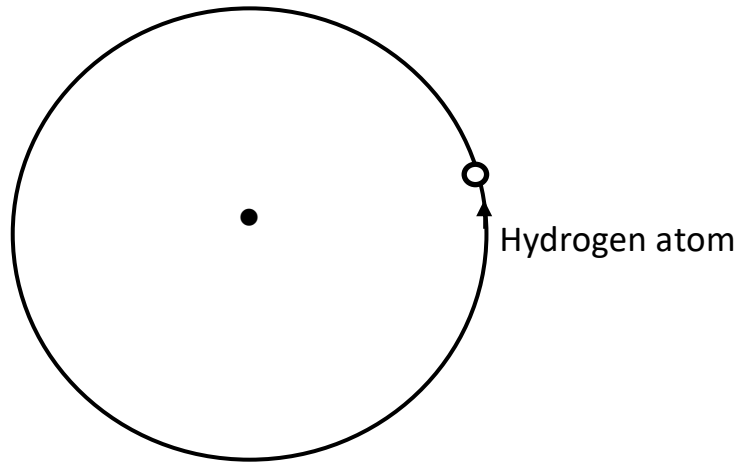
1. Speed of sound in water \sim 4900 ft/sec
2. 1 Nautical mile \sim 6000 ft.



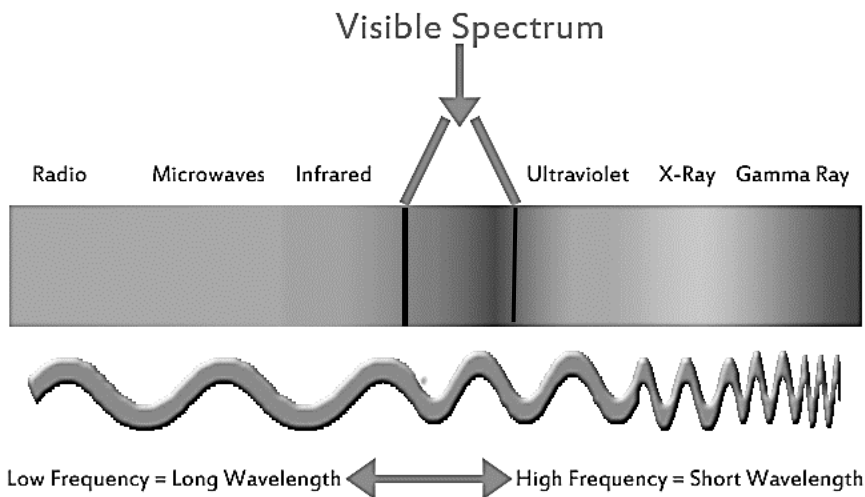
Soviet submarine with US Navy P-3 Orion
anti-submarine surveillance aircraft
(My old alma mater – Patrol Squadron Eight!)

Structure of the atom and the nature of light

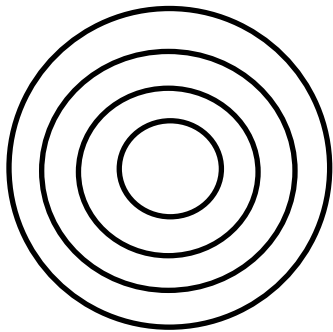
Recall:



De Broglie Wavelength



Wile E. Coyote's Last Hurrah!



Hubble Law

Hubble's law or **Hubble—Lemaître's law** is the name for the observation that:

1. All objects observed in deep space (extragalactic space, ~ 10 Mpc or more) have a doppler shift-measured velocity relative to Earth, and to each other;
2. The doppler-shift-measured velocity of galaxies moving away from Earth, is proportional to their distance from the Earth and all other interstellar bodies.

In effect, the space-time volume of the observable universe is expanding and Hubble's law is the direct physical observation of this. It is the basis for believing in the **expansion of the universe** and is evidence often cited in support of the Big Bang model.

Although widely attributed to Edwin Hubble, the law was first derived from the General Relativity equations by Georges Lemaître in a 1927 article. There he proposed that the Universe is expanding, and suggested a value for the rate of expansion, now called the **Hubble constant**. Two years later Edwin Hubble confirmed the existence of that law and determined a more accurate value for the constant that now bears his name. The recession velocity of the objects was inferred from their redshifts, many measured earlier by Vesto Slipher in 1917 and related to velocity by him.

The law is often expressed by the equation $v = H_0 D$, with H_0 the constant of proportionality (the **Hubble constant**) between the "proper distance" D to a galaxy and its velocity v (see *Uses of the proper distance*). H_0 is usually quoted in (km/s)/Mpc, which gives the speed in km/s of a galaxy 1 megaparsec (3.09×10^{19} km) away. The reciprocal of H_0 is the Hubble time.

Hubble law: $V = H_0 D$

Where:

V = velocity in Km/sec

H_0 = Hubble Constant = $\frac{71 \text{ Km/sec}}{\text{Mpc}}$

D = distance in parsecs (pc)

1 parsec (pc) = 3.26 LY

Example:

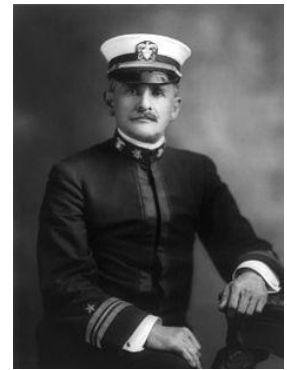
Astronomers observe a galaxy 7 billion light years away.

1. How fast is the galaxy moving away from us?
2. How long has it been travelling?

Michelson – Morley Experiment

Albert Michelson

1. _____
2. _____

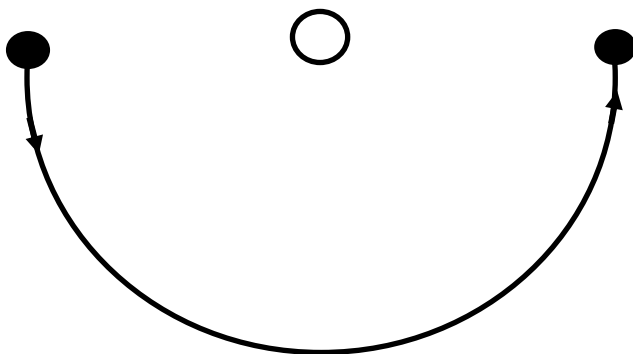
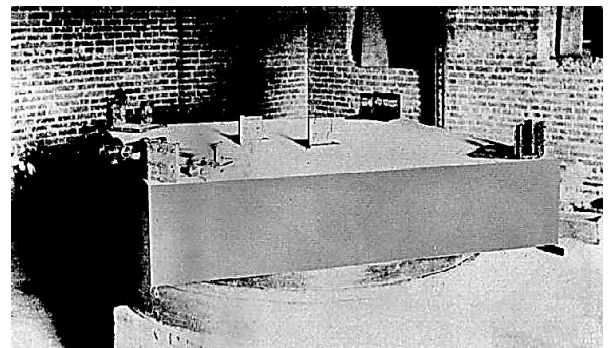
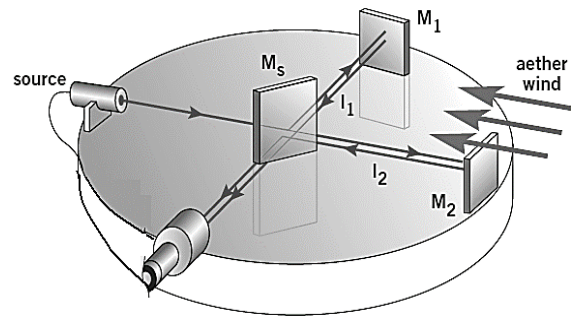


Luminiferous Ether (Aether) (the “Ether”)

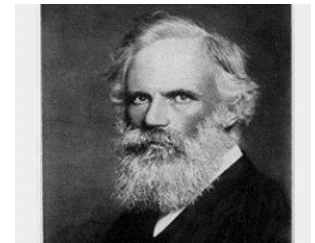
1. _____
2. _____

Michelson-Morley Experiment

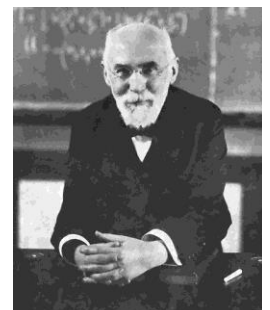
- As the earth moves through the ether, the “wind” will act like the river current, affecting the motion of the light waves.
- Rotating the experiment will cause interference fringes to change, proving the existence of the ether.



George Fitzgerald _____



Hendrik Lorentz : _____



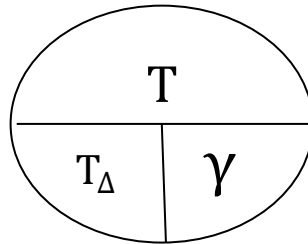
Lorentz Factor: $\sqrt{1 - \frac{v^2}{c^2}}$ or γ ("Gamma")

Where

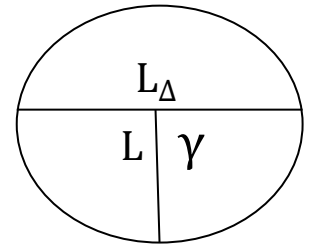
Time: $T_{\Delta} = \frac{T}{\sqrt{1 - \frac{v^2}{c^2}}}$

Length: $L = L_{\Delta} \times \sqrt{1 - \frac{v^2}{c^2}}$

or $T_{\Delta} = \frac{T}{\gamma}$



or $L_{\Delta} = L \times \gamma$



Relativity Toolbox

Where:

$T_{\Delta} =$ _____

$T =$ _____

$C =$ _____

$V =$ _____

$L_{\Delta} =$ _____

$L =$ _____

Relativistic Velocities (_____)

Non-Relativistic Velocities (_____)

"Gamma" (γ) is the factor that allows us to compute _____ in both _____ and _____ given a specific velocity; these effects are most evident at _____, but occur at any and all velocities.

Einstein's Two Postulates of Special Relativity:

1. The laws of physics _____ _____
2. The speed of light _____ _____

Quotes by Albert Einstein:

On Relativity:

“When you are courting a nice girl, an hour seems like a second. When you sit on a red - hot cinder, a second seems like an hour. That's relativity.”

On virtue:

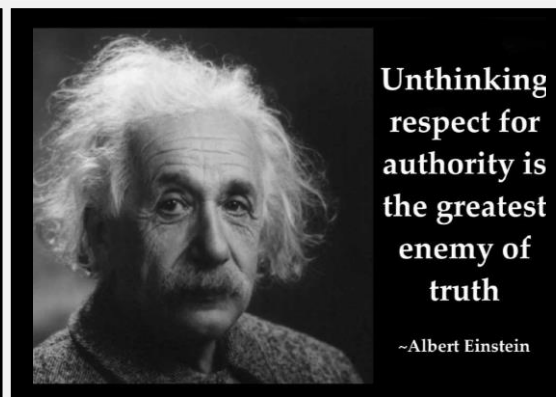
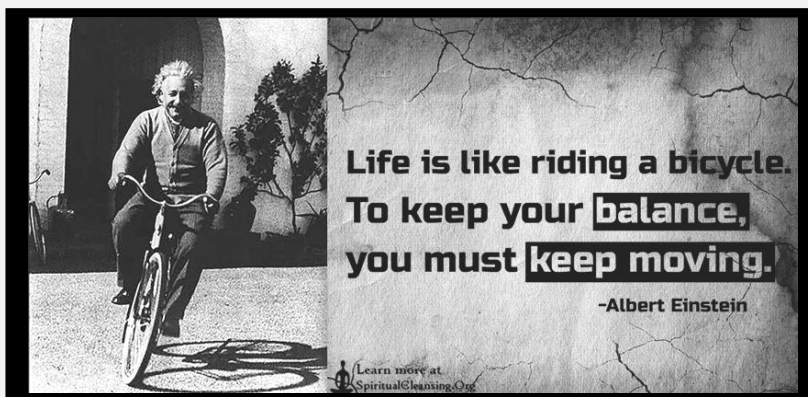
“As far as I'm concerned, I prefer silent vice to ostentatious virtue.”

On traffic safety:

“Any man who can drive safely while kissing a pretty girl is simply not giving the kiss the attention it deserves.”

On nationalism:

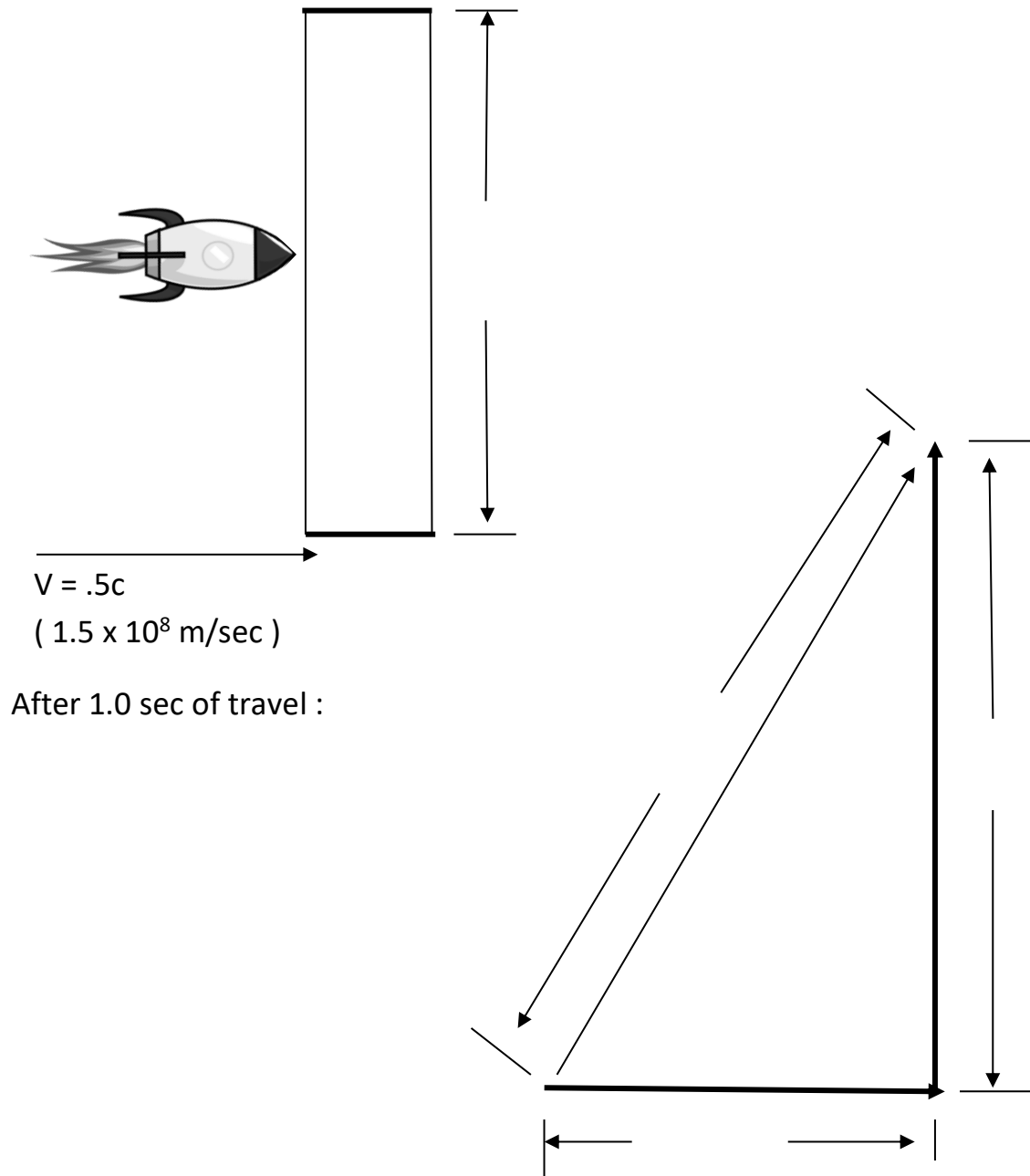
“Nationalism is an infantile disease. It is the measles of mankind.”



To understand why Relativity is necessary we have to look at the practical problems resulting from a Cosmic Speed Limit (The speed of light: "c")

(C= 186,000 mi/sec, 300,000 km/sec, and/or 3.0×10^8 m/sec)

We'll start with a ridiculous imaginary clock:

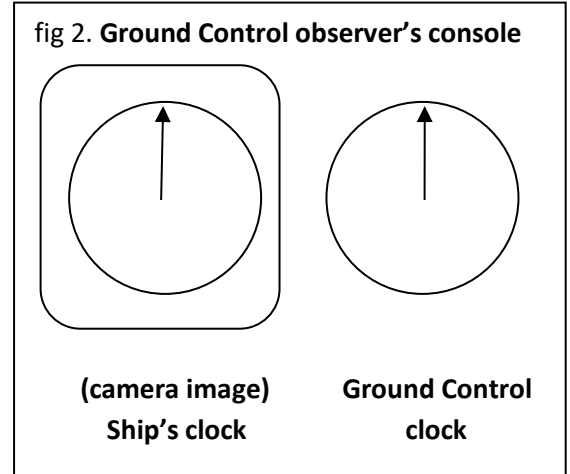
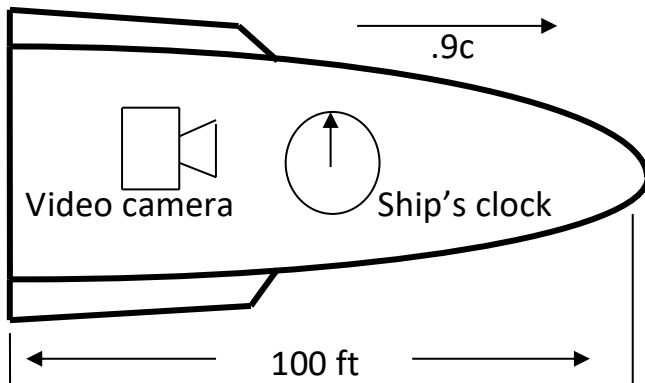


Relativity Example 1.

A spacecraft passes NASA Ground Control at .9c.

A video camera monitors the clock inside the cabin and transmits the image to an observer in Ground Control. The observer has his own clock adjacent to the console video screen displaying the shipboard clock.

fig. 1



Question 1: The Ground Controller observes the image of the Ship's clock second hand as it completes 1 rotation (60 sec). How much time has elapsed on the Ground Control clock?

Step 1: Calculate "Gamma" (γ)

$$\gamma = \sqrt{1 - \frac{v^2}{c^2}}$$

Step 2: Solve for T_{Δ}

$$T_{\Delta} = \frac{T}{\gamma}$$

Question 2: What is the length of the spacecraft from the perspective of the observer?

$$L = L_{\Delta} \times \gamma$$

Relativity and the Muon

Evidence supporting Einstein's theory of Special Relativity is found in the analysis of the behavior of *muons*.

Muons are subatomic particles that are created in Earth's upper atmosphere when cosmic rays (typically protons) collide with the nuclei of air molecules; muons have a velocity of .998c and a "life span" of 2.2×10^{-6} seconds (*at rest*), after which they disintegrate into other particles.

Scientists conducted an experiment in which they detected the presence of muons at the top of Mount Washington, New Hampshire.

After recording their results, they then moved their detection equipment to a New England beach ("sea level").

Given the altitude of Mt. Washington (**approximately 2000 meters**), and the velocity (V) and "life span" (T) of muons, (and discounting the effects of Relativity) there should have been no muons detected at sea level, since :

$$\begin{array}{ccc}
 (V) \times (T) = & \xrightarrow{\hspace{10em}} & (\text{Distance}) \\
 \downarrow & & \downarrow \\
 (.998c) \times (2.2 \times 10^{-6}) = & (2.994 \times 10^8 \text{ m/sec}) (2.2 \times 10^{-6} \text{ sec}) = & 658.68 \text{ meters}
 \end{array}$$

In other words, according to classical Newtonian principles the muons should have disintegrated a little over a third of the distance down from the top of the mountain.

Yet, when the detection equipment was activated at sea level, muons were clearly and abundantly present!

Solution:

1. Calculate "Gamma" for .998c

2. Calculate T_{Δ}

3. Calculate L_{Δ} *from the perspective of the muon:*

Famous quotes by baseball legend and American philosopher Yogi Berra:

On Relativistic Time:

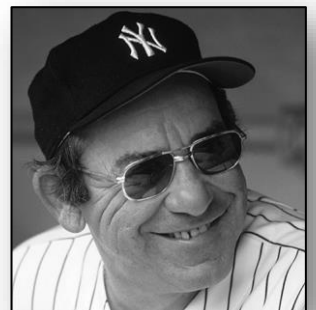
“This is the earliest I’ve ever been late!”

On Quantum Physics:

“When you come to a fork in the road, take it.”

On the Abstract Mathematics:

“Baseball is ninety percent mental and the other half is physical.”



The Twins Paradox

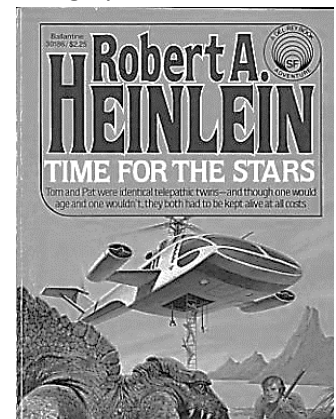
One of pair of identical twins is selected to be a crew member of a deep-space expedition to a star eleven light-years distant.

The other twin will remain on Earth.

The vessel will travel at $.998c$

Discounting the time spent exploring the star system, determine the ages of each twin upon the vessel's return to Earth

This one is a lot of fun, written in the 50's. It's all about the Twins Paradox. Highly recommended!



Gamma Chart For Relativistic Velocities

v	v^2	$1-v^2$	$\sqrt{(1-v^2)}$ (" γ ")
.9c (.1 or one-tenth under "c")	.81	.19	.44
.99c (.01 or one-hundredth under "c")	.980	.02	.14
.999c (.001 or one-thousandth under "c")	.998	.002	.045
.9999c (.0001 or one-ten thousandth under "c")	.9998	.0002	.014
.99999c (.00001 or one-hundred thousandth under "c")	.99998	.00002	.0045
.999999c (.000001 or one-millionth under "c")	.999998	.000002	.0014
.9999999c (.0000001 or one-ten millionth under "c")	.9999998	.0000002	.00045
.99999999c (.00000001 or one-hundred millionth under "c")	.99999998	.00000002	.00014
.999999999c (.000000001 or one-billionth under "c")	.999999998	.000000002	.000045
.9999999999c (.0000000001 or one-ten billionth under "c")	.9999999998	.0000000002	.000014

Further Problems with Relativistic Travel (example 1):

A crew of astronauts leaves Earth to explore deep space.

Given:

1. From the crew's perspective, they will experience one year of shipboard time travelling within a billionth of "c".
2. "Gamma" for their velocity is 0.00001 (See chart on previous page)

Determine how much time will have elapsed on Earth when they return.

Further Practical Problems with Relativistic Velocity (Example 2)

Given: A space vessel traveling at $.9c$ collides with a small object with a mass of grain of salt, approximately 5.86×10^{-8} Kg

How much kinetic energy (KE) is released at impact?

(Comparison: 1 ton of TNT = 4.2×10^9 Joules)

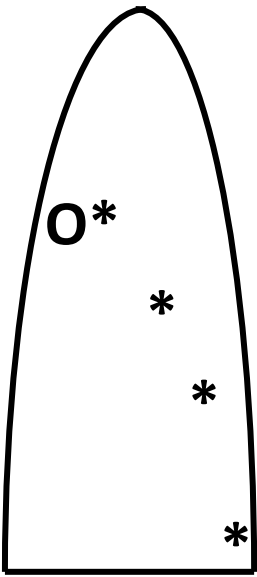
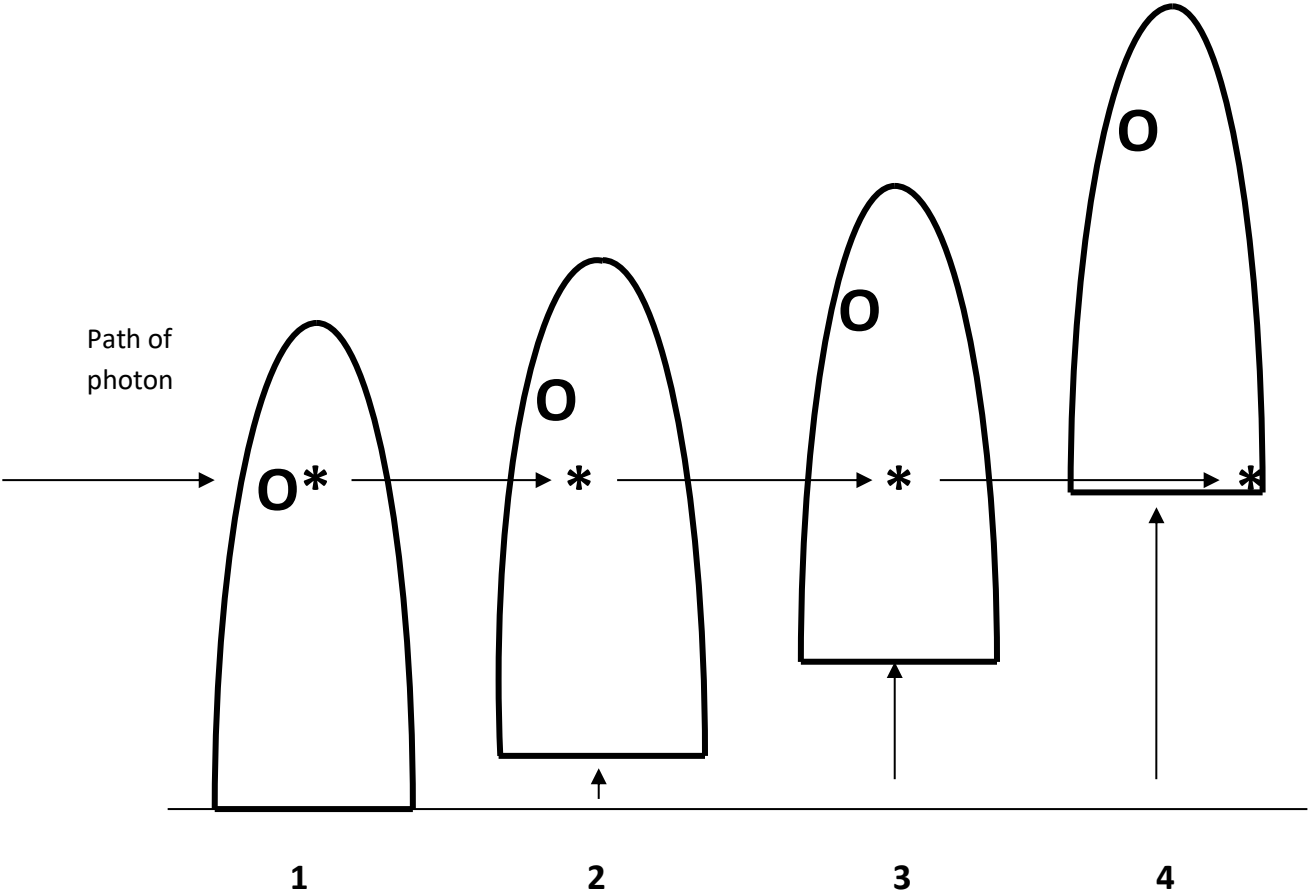
Further Practical Problems with Relativistic Velocity (Example 3)

Given: A space vessel traveling at $.9c$ collides with an small object with a mass of 2.5 grams (roughly the mass of a penny)

How much kinetic energy (KE) is released at impact?

(Comparison: The energy released by atomic bomb detonated over Hiroshima was approximately 6.5×10^{13} J or 65,000,000,000,000 or 65 thousand billion Joules)

The effects of acceleration on the path of a photon



Path of photon relative to spacecraft

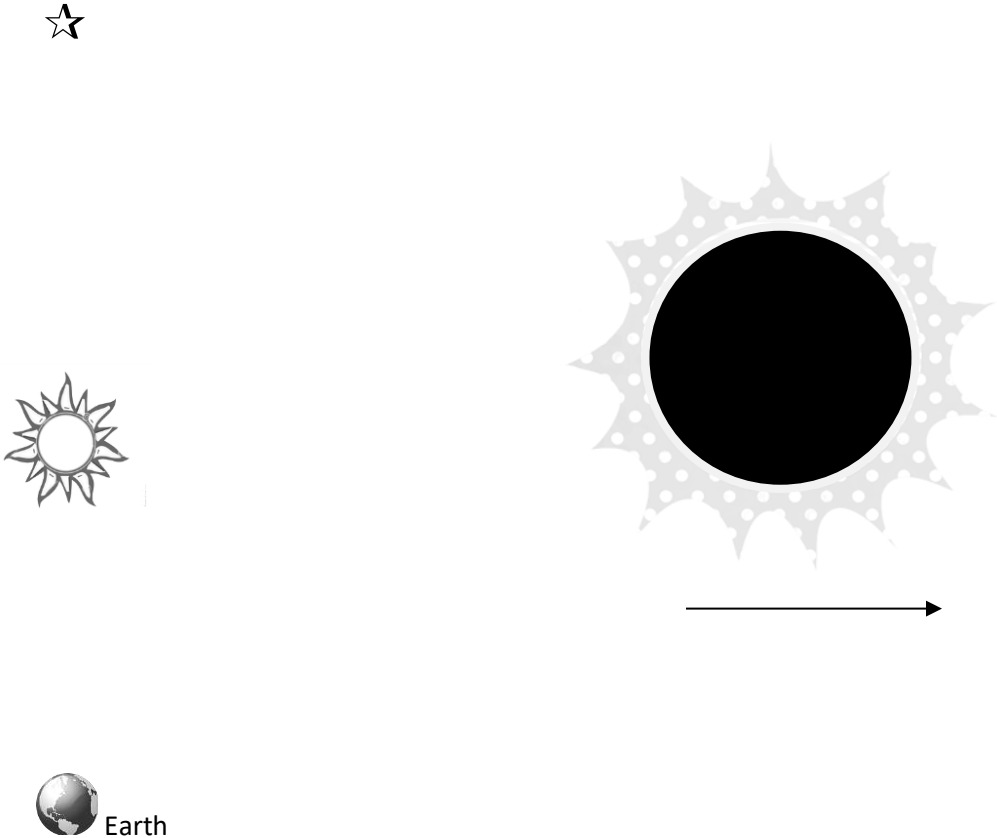
An Einstein “Thought Experiment”

If the Sun was to suddenly vanish, would the Earth break from its orbit at the instance of the Sun’s disappearance?

Newton’s View

Einstein’s view:

Proof of gravity affecting light during solar eclipse:



Another Thought Experiment:

Escape Velocity:

Formula for Escape Velocity:

$$V_{esc} = \sqrt{\frac{2GM}{r}}$$

Calculate Escape Velocity (V_{esc}) for Earth

Data:

Radius of Earth: 6378 Km

Mass of Earth: 6.0×10^{24} Kg

Universal Gravitational Constant (G): 6.672×10^{-11}

Now let's super- shrink the Earth and reduce the radius to 7.8 mm (7.8×10^{-3} m) and calculate the new escape velocity.

Approx. actual size:



The Most Famous Equation in the World:

$$E = mc^2$$

To get a handle on this, let's first take a look at a lesser known version:

$$E = mc^2$$

Where:

E = "Binding Energy"

m = "mass defect"

C² = speed of light squared (3.0 x 10⁸)²

Data:
Mass of a proton = 1.67262 x 10 ⁻²⁷ Kg
Mass of a neutron = 1.67493 x 10 ⁻²⁷ Kg
Mass of an electron = 9.1094 x 10 ⁻³¹ Kg

We'll start by constructing a Helium atom and predicting its mass based on the known masses of its constituent parts.

Remember, a Helium atom contains 2 protons, 2 neutrons, and 2 electrons

${}^4_2\text{H}$ compared to ${}^{235}_{92}\text{U}$
Top# _____
Botton# _____

2 protons _____ Kg
+ 2 neutrons _____ Kg

Predicted total = _____ Kg

Actual total = 6.6463 x 10⁻²⁷ Kg

Difference: _____ Kg
(Missing mass or "_____")

$$E = mc^2$$

= _____ x _____
= _____ x _____
= _____ Joules

Now compare the mass – energy conversion factor:

Original mass _____

Resulting energy _____

Note the exponential difference

Finally, **$E = mc^2$**

An alternate way to read the formula:

“There is an equivalence between mass and energy, with a conversion factor that is the square of the speed of light”

Question:

How much TOTAL energy is contained in 1 Kilogram of material (like the Laboratory Rock)?

BOOM!

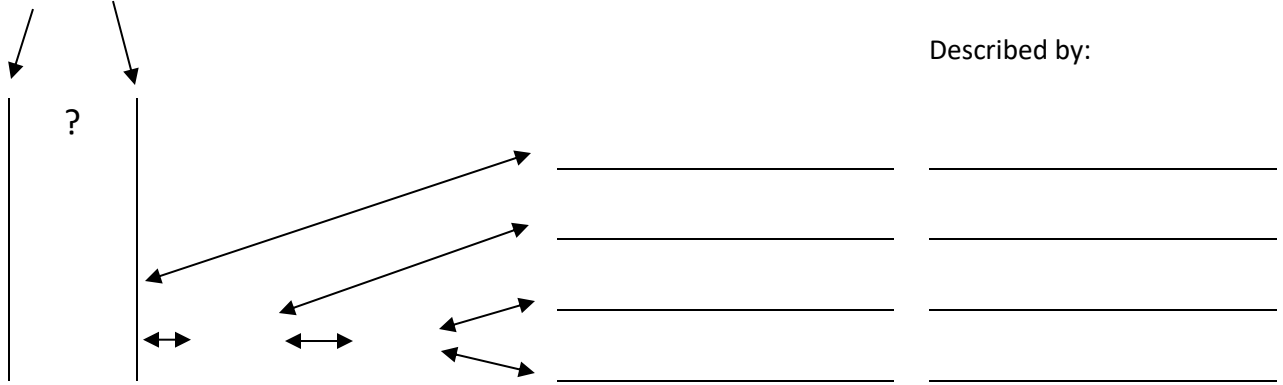


Epilogue: Where do we go from here?

The Four Fundamental Forces:

B.B.

0 sec - 10^{-43} sec



Conflict: The existence of _____

String Theory – possible solution?

All “matter” is _____

Original model called for the existence of _____

Problems developed because of mathematical _____

Anomalies resolved by _____

Strength of String Theory: _____

Weakness of String Theory: _____

